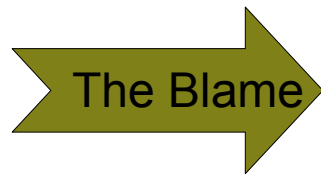
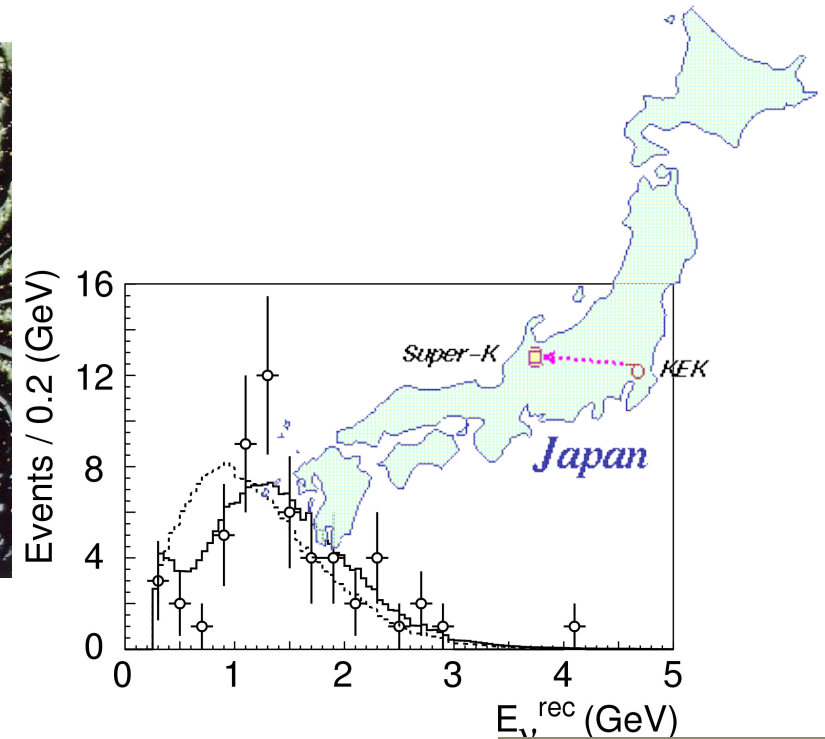
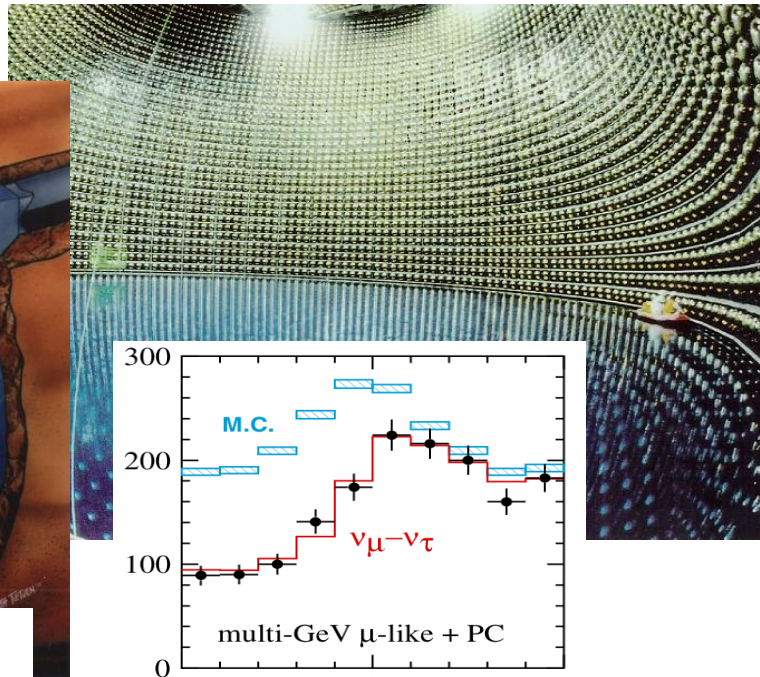


Studies of Alternatives to Neutrino Oscillation using Super-K Atmospheric Neutrino Data

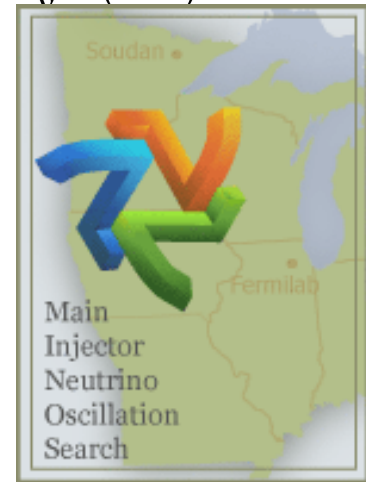
Wei Wang
Boston University
Brookhaven National Lab, Feb 8, 2007

An Era of Discovery in Neutrino Physics



$$\begin{pmatrix} \nu_\alpha \\ \nu_\beta \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_{m_a} \\ \nu_{m_b} \end{pmatrix}$$

$$\rightarrow P_{\nu_\alpha \rightarrow \nu_\alpha} = 1 - \sin^2 2\theta \sin^2 \frac{\Delta m^2 L}{4E}$$

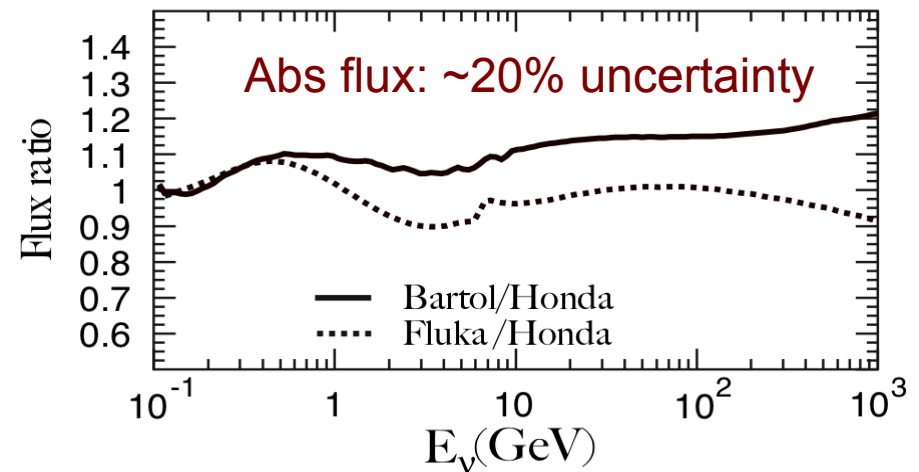
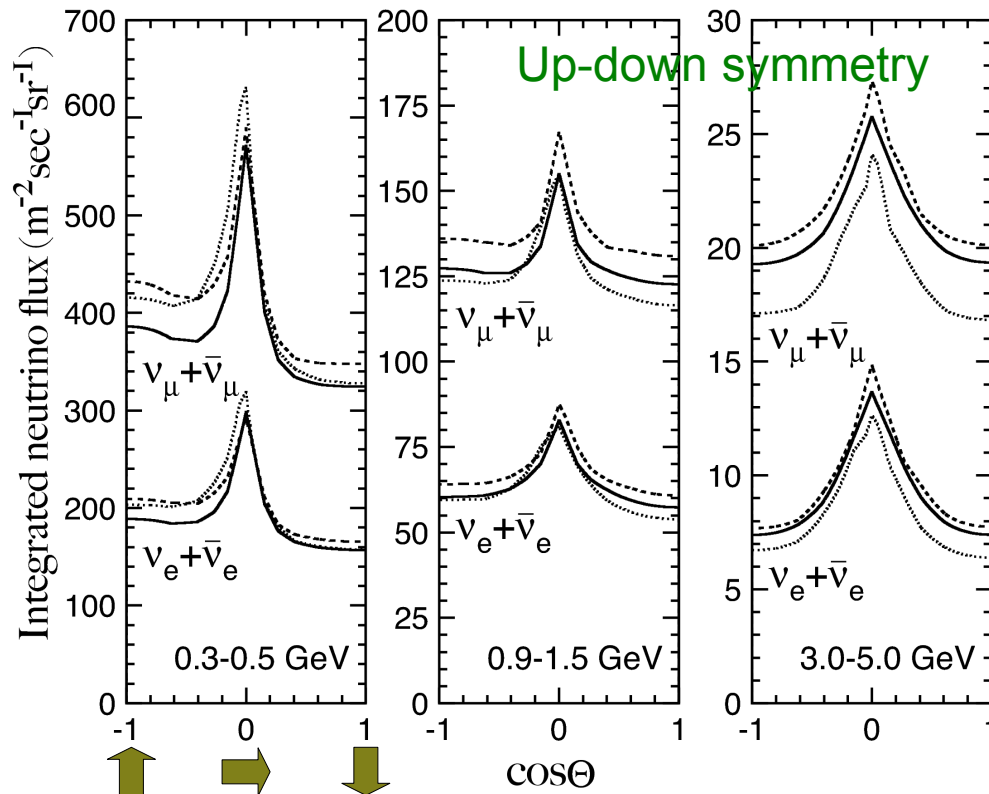
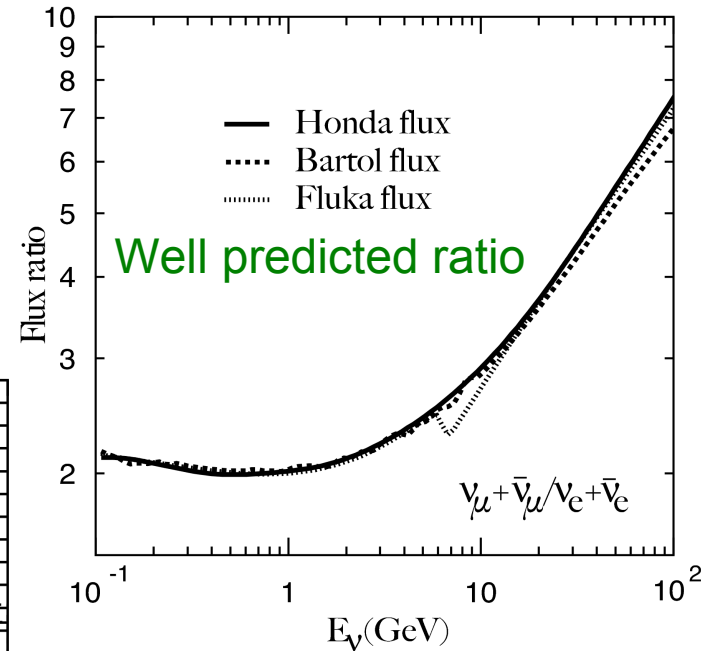
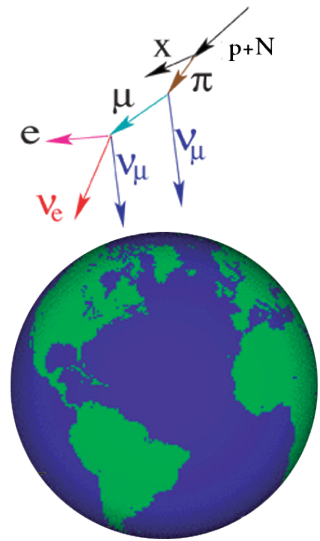


Outline

- ♦ Atmospheric neutrinos, Super-K experiment and events
- ♦ Standard ν_{μ} - ν_{τ} oscillation analysis
- ♦ Sterile neutrino as a alternative to tau neutrino
 - ν_{μ} - ν_{τ} mixing vs ν_{μ} - ν_s mixing
 - An admixture analysis
- ♦ Neutrino oscillations induced by the violations of Lorentz (LIV) and CPT (CPTV) invariance
 - Plausibility and allowed limits
- ♦ Vanishing neutrinos caused by neutrino decoherence and neutrino decay
 - Plausibility and allowed limits
- ♦ Summary and conclusions

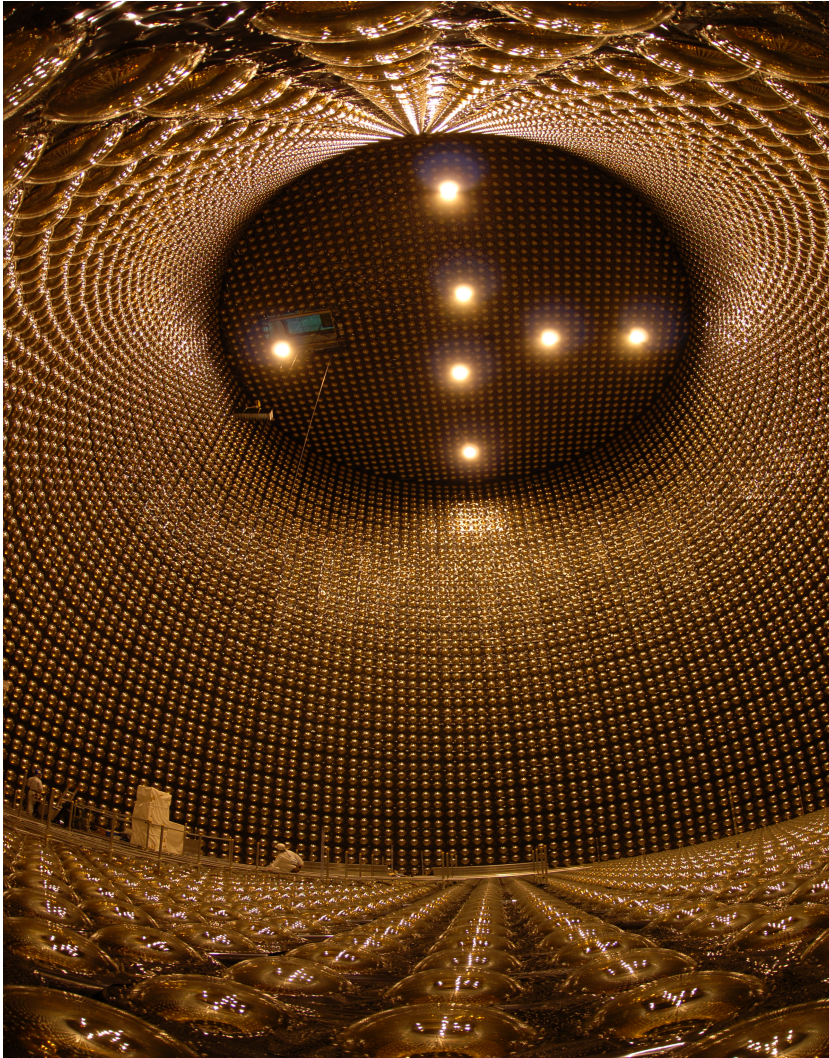
Atmospheric Neutrinos

- A large uncertainty on the absolute flux
- Good knowledge on flavor ratio 😊
- Up-down symmetric 😊



Super-Kamiokande Collaboration

- 140 collaborators from 35 institutes of 5 countries



S. Fukuda,¹ Y. Fukuda,¹ M. Ishitsuka,¹ Y. Itow,¹ T. Kajita,¹ J. Kameda,¹ K. Kaneyuki,¹ K. Kobayashi,¹ Y. Koshio,¹ M. Miura,¹ S. Moriyama,¹ M. Nakahata,¹ S. Nakayama,¹ Y. Obayashi,¹ A. Okada,¹ K. Okumura,¹ N. Sakurai,¹ M. Shiozawa,¹ Y. Suzuki,¹ H. Takeuchi,¹ Y. Takeuchi,¹ T. Toshito,¹ Y. Totsuka,¹ S. Yamada,¹ M. Earl,² A. Habig,^{2,*} E. Kearns,² M. D. Messier,² K. Scholberg,² J. L. Stone,² L. R. Sulak,² C. W. Walter,² M. Goldhaber,³ T. Barszczak,⁴ D. Casper,⁴ W. Gajewski,⁴ W. R. Kropp,⁴ S. Mine,⁴ L. R. Price,⁴ M. Smy,⁴ H. W. Sobel,⁴ M. R. Vagins,⁴ K. S. Ganezer,⁵ W. E. Keig,⁵ R. W. Ellsworth,⁶ S. Tasaka,⁷ A. Kibayashi,⁸ J. G. Learned,⁸ S. Matsuno,⁸ D. Takemori,⁸ Y. Hayato,⁹ T. Ishii,⁹ T. Kobayashi,⁹ K. Nakamura,⁹ Y. Oyama,⁹ A. Sakai,⁹ M. Sakuda,⁹ O. Sasaki,⁹ M. Kohama,¹⁰ A. T. Suzuki,¹⁰ T. Inagaki,¹¹ K. Nishikawa,¹¹ T. J. Haines,^{12,4} E. Blaufuss,¹³ B. K. Kim,¹³ R. Sanford,¹³ R. Svoboda,¹³ M. L. Chen,¹⁴ J. A. Goodman,¹⁴ G. Guillian,¹⁴ G. W. Sullivan,¹⁴ J. Hill,¹⁵ C. K. Jung,¹⁵ K. Martens,¹⁵ M. Malek,¹⁵ C. Mauger,¹⁵ C. McGrew,¹⁵ E. Sharkey,¹⁵ B. Viren,¹⁵ C. Yanagisawa,¹⁵ M. Kirisawa,¹⁶ S. Inaba,¹⁶ C. Mitsuda,¹⁶ K. Miyano,¹⁶ H. Okazawa,¹⁶ C. Saji,¹⁶ M. Takahashi,¹⁶ M. Takahata,¹⁶ Y. Nagashima,¹⁷ K. Nitta,¹⁷ M. Takita,¹⁷ M. Yoshida,¹⁷ S. B. Kim,¹⁸ T. Ishizuka,¹⁹ M. Etoh,²⁰ Y. Gando,²⁰ T. Hasegawa,²⁰ K. Inoue,²⁰ K. Ishihara,²⁰ T. Maruyama,²⁰ J. Shirai,²⁰ A. Suzuki,²⁰ M. Koshihara,²¹ Y. Hatakeyama,²² Y. Ichikawa,²² M. Koike,²² K. Nishijima,²² H. Fujiyasu,²³ H. Ishino,²³ M. Morii,²³ Y. Watanabe,²³ U. Golebiewska,²⁴ D. Kielczewska,^{24,4} S. C. Boyd,²⁵ A. L. Stachyra,²⁵ R. J. Wilkes,²⁵ and K. K. Young^{25,†}

(Super-Kamiokande Collaboration)

¹Institute for Cosmic Ray Research, University of Tokyo, Kashiwa, Chiba 277-8582, Japan

²Department of Physics, Boston University, Boston, Massachusetts 02215

³Physics Department, Brookhaven National Laboratory, Upton, New York 11973

⁴Department of Physics and Astronomy, University of California at Irvine, Irvine, California 92697-4575

⁵Department of Physics, California State University, Dominguez Hills, Carson, California 90747

⁶Department of Physics, George Mason University, Fairfax, Virginia 22030

⁷Department of Physics, Gifu University, Gifu, Gifu 501-1193, Japan

⁸Department of Physics and Astronomy, University of Hawaii, Honolulu, Hawaii 96822

⁹Institute of Particle and Nuclear Studies, High Energy Accelerator Research Organization (KEK), Tsukuba, Ibaraki 305-0801, Japan

¹⁰Department of Physics, Kobe University, Kobe, Hyogo 657-8501, Japan

¹¹Department of Physics, Kyoto University, Kyoto 606-8502, Japan

¹²Physics Division, P-23, Los Alamos National Laboratory, Los Alamos, New Mexico 87544

¹³Department of Physics and Astronomy, Louisiana State University, Baton Rouge, Louisiana 70803

¹⁴Department of Physics, University of Maryland, College Park, Maryland 20742

¹⁵Department of Physics and Astronomy, State University of New York, Stony Brook, New York 11794-3800

¹⁶Department of Physics, Niigata University, Niigata, Niigata 950-2181, Japan

¹⁷Department of Physics, Osaka University, Toyonaka, Osaka 560-0043, Japan

¹⁸Department of Physics, Seoul National University, Seoul 151-742, Korea

¹⁹Department of Systems Engineering, Shizuoka University, Hamamatsu, Shizuoka 432-8561, Japan

²⁰Research Center for Neutrino Science, Tohoku University, Sendai, Miyagi 980-8578, Japan

²¹The University of Tokyo, Tokyo 113-0033, Japan

²²Department of Physics, Tokai University, Hiratsuka, Kanagawa 259-1292, Japan

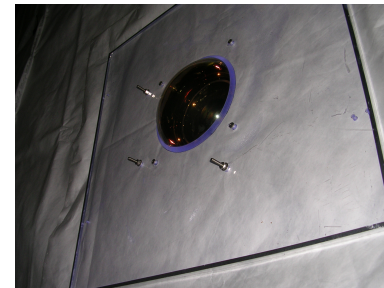
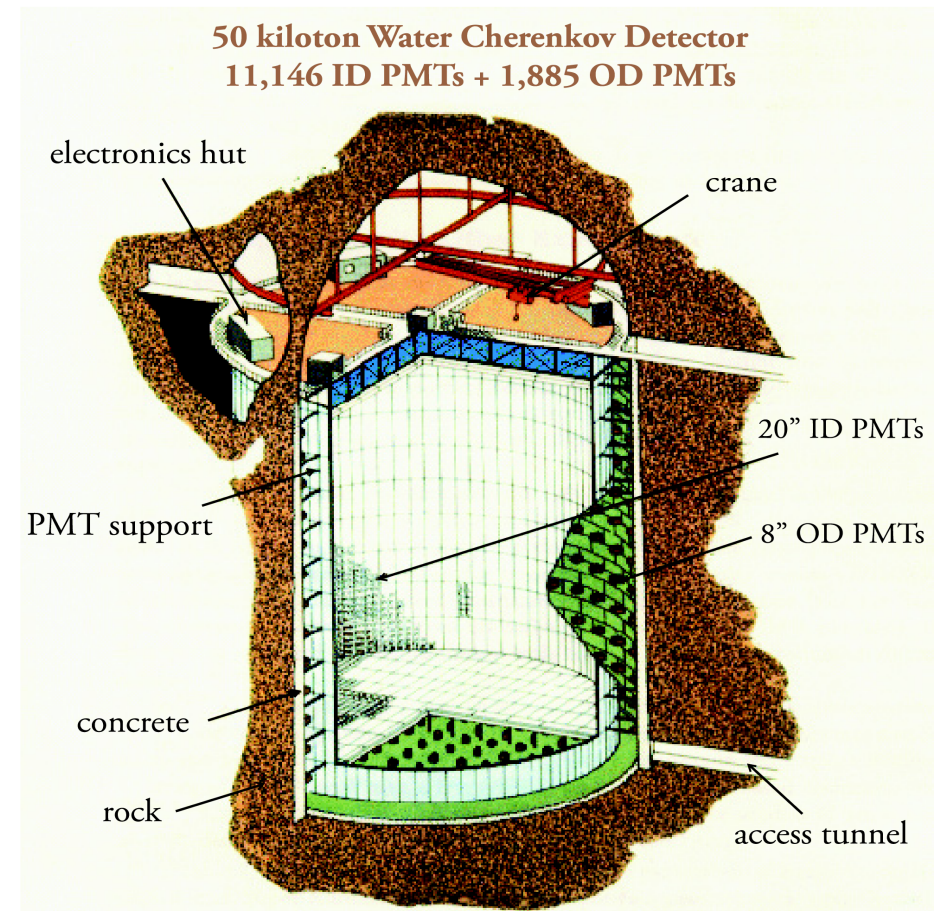
²³Department of Physics, Tokyo Institute of Technology, Meguro, Tokyo 152-8551, Japan

²⁴Institute of Experimental Physics, Warsaw University, 00-681 Warsaw, Poland

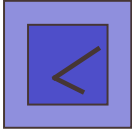

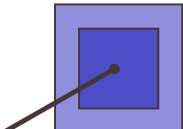
²⁵Department of Physics, University of Washington, Seattle, Washington 98195-1560

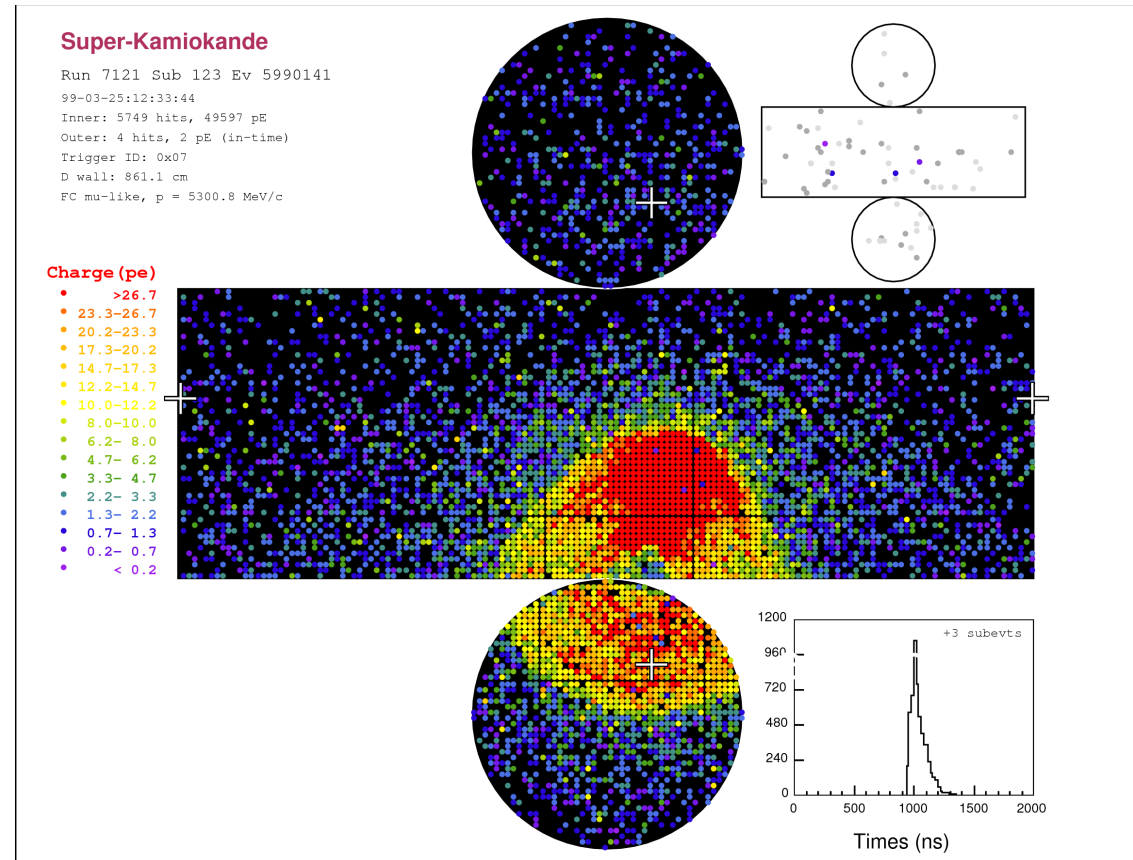
Super-Kamiokande Experiment

- A 50 kt water Cherenkov detector
 - Inner detector and outer detector optically separated
 - ID: 25in PMTs; gaps filled by black sheet
 - OD: 8 inch PMTs with wavelength shifters, wall covered by reflective Tyvek
- Operating periods
 - **SK-I: 1996 – 2001**
 - ✓ 1489 days livetime
 - ✓ ~40% ID coverage
 - **SK-II: 2003 – 2005**
 - ✓ 804 days livetime
 - ✓ Half ID tubes (acrylic cover & FRP), ~20% coverage
 - **SK-III: since Summer 2006**
 - ✓ ID tubes (acrylic cover & FRP) fully recovered



Neutrino Events

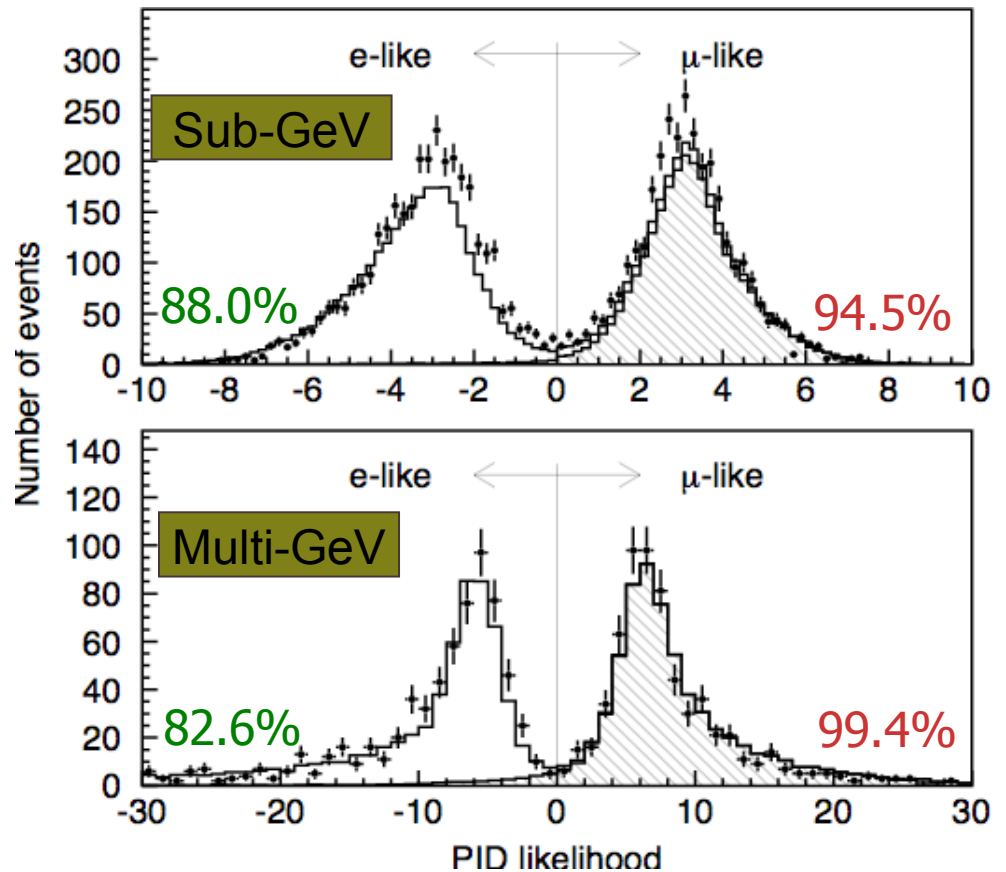
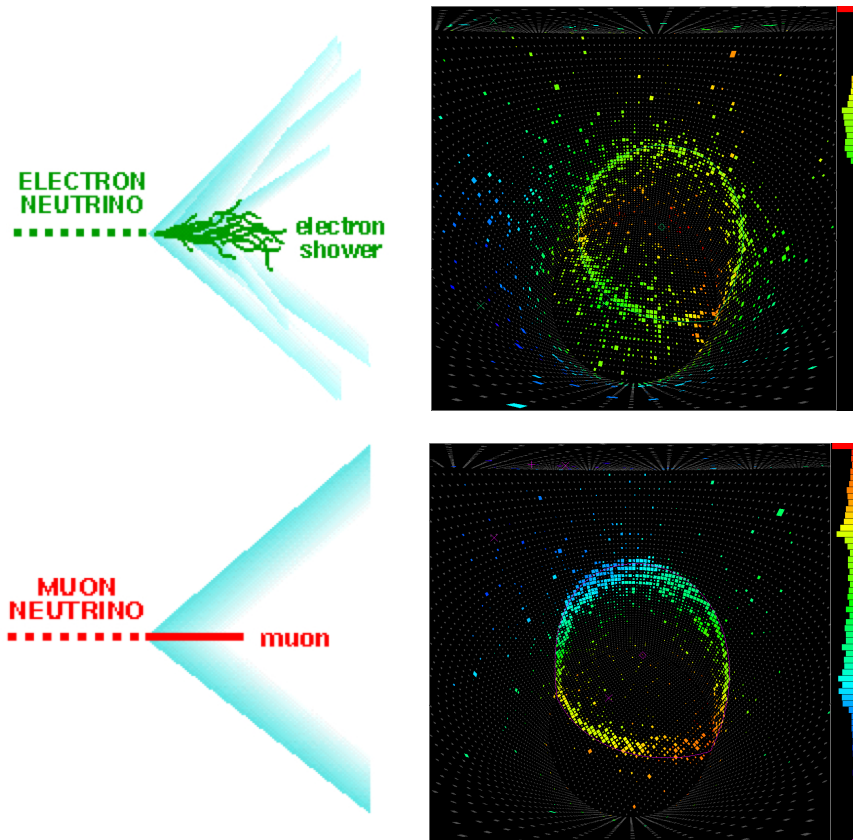
- Neutrino interaction
 - charged particles
 - Cherenkov radiation
 - recorded by PMTs
- Super-K event categories
 - Fully contained 
 - Partially contained 
 - Upward going μ 



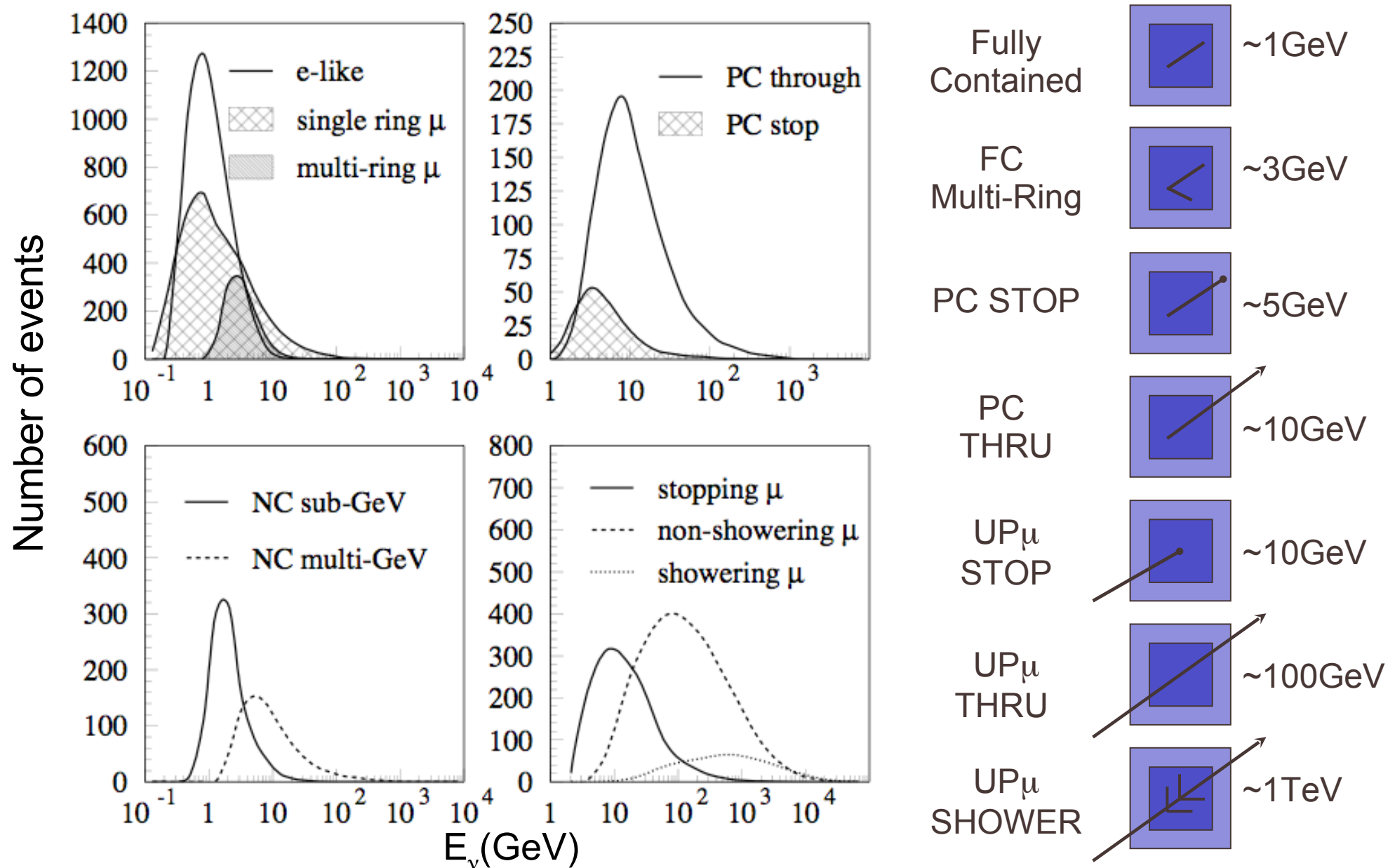
Event Reconstruction

- Vertex finding
- Ring recognition
- **PID (e-/ μ -like)**
- Momentum reconstruction

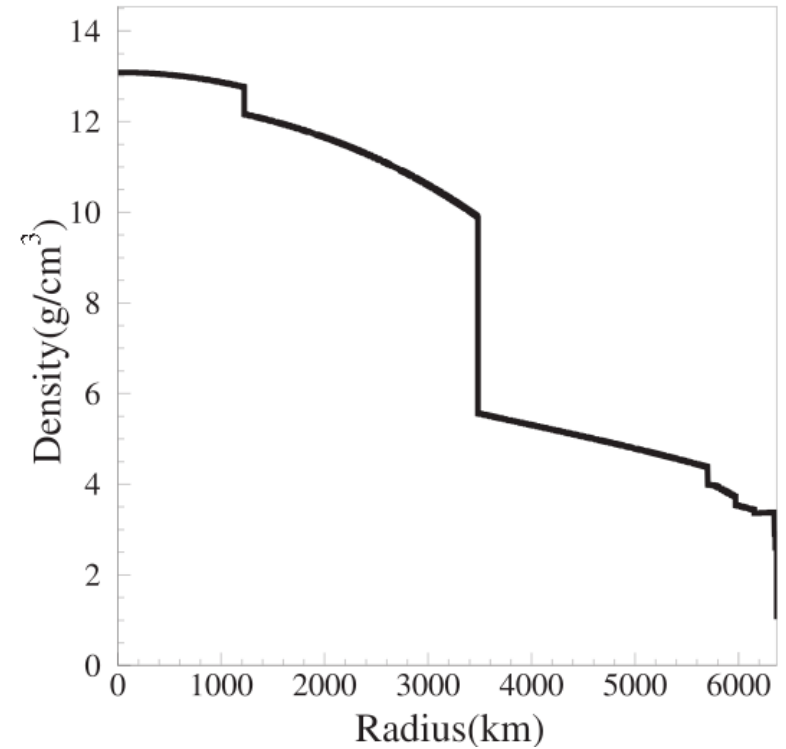
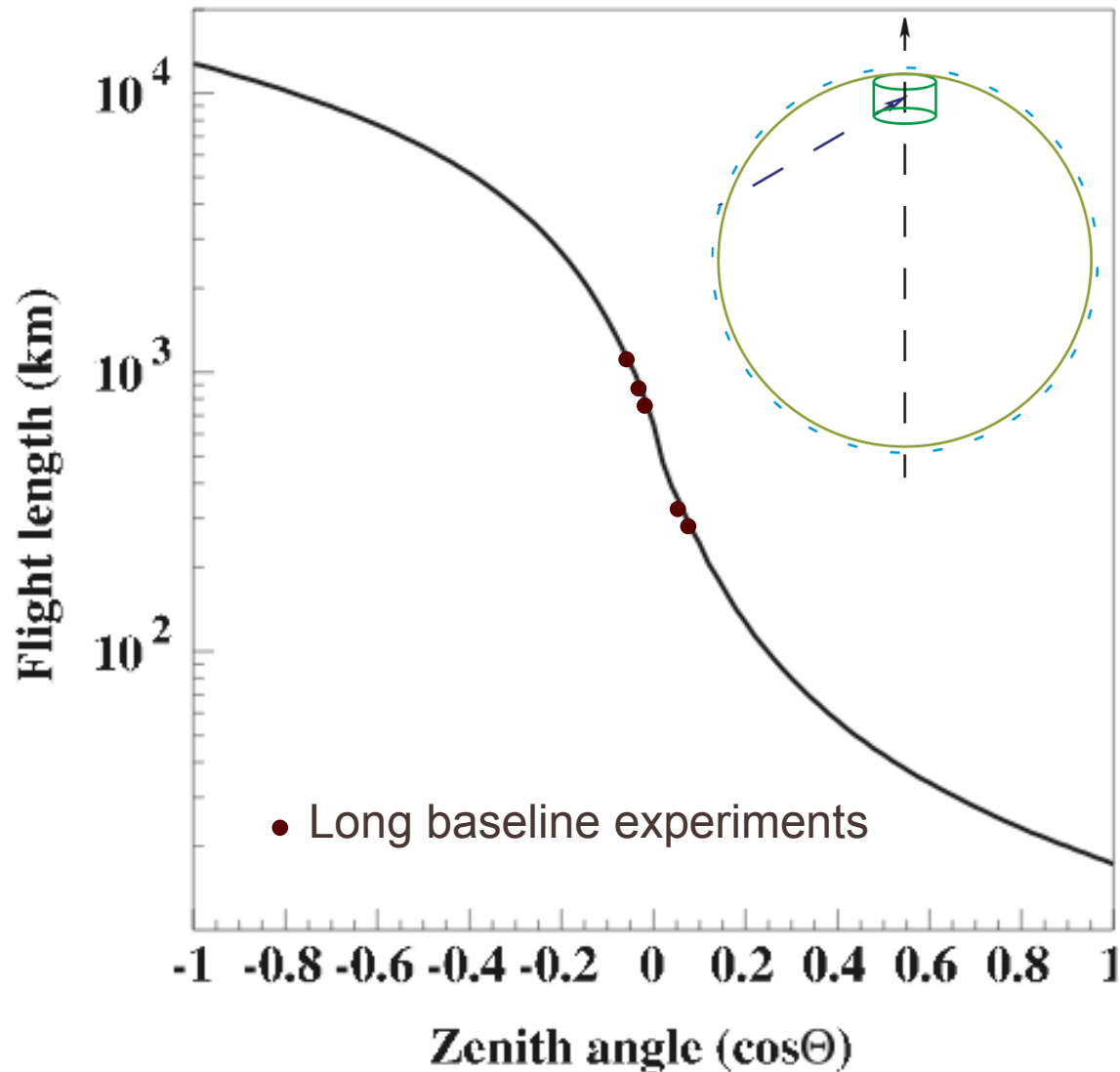
FC Single Ring Events



Five Decades of Energy



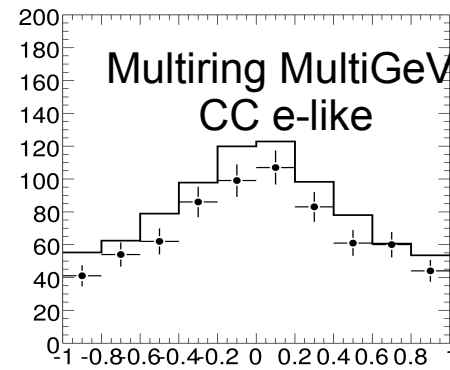
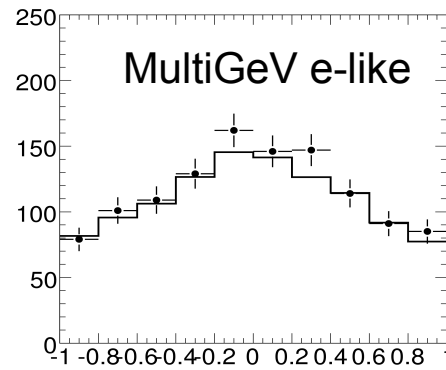
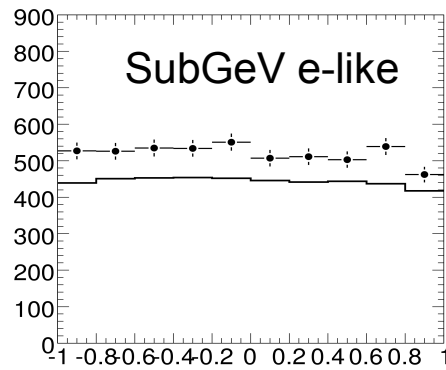
Four Decades of Pathlengths



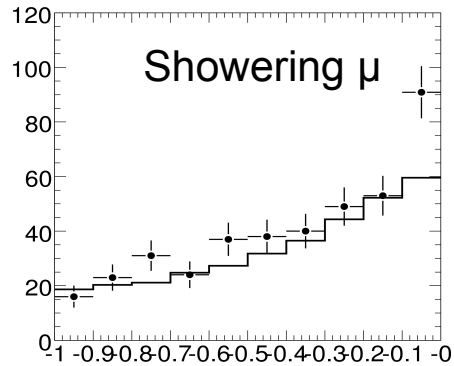
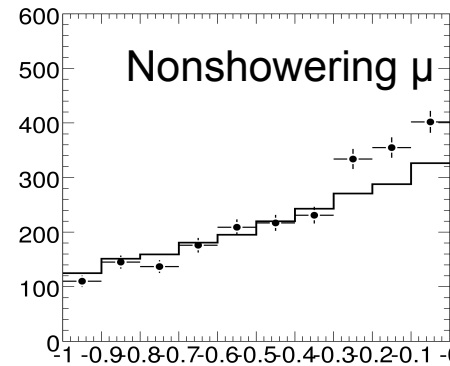
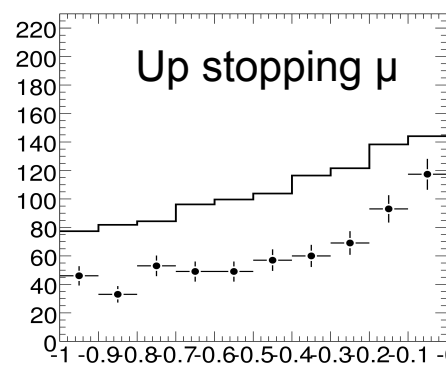
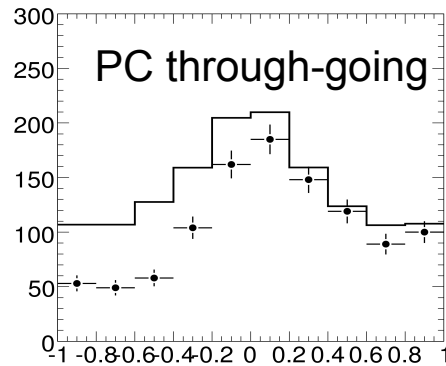
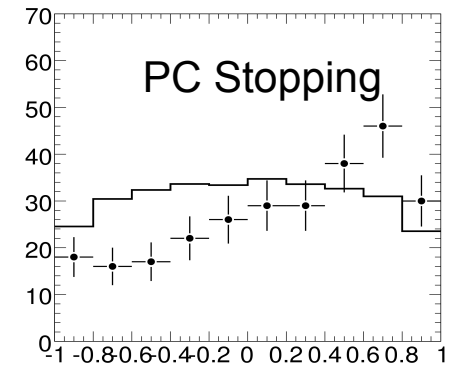
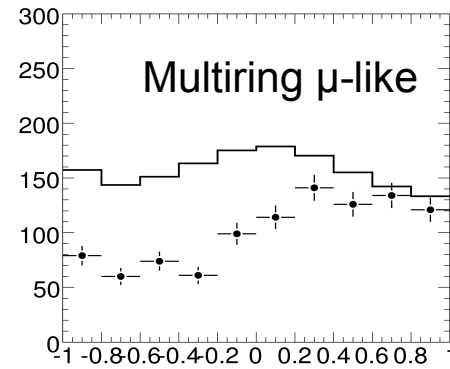
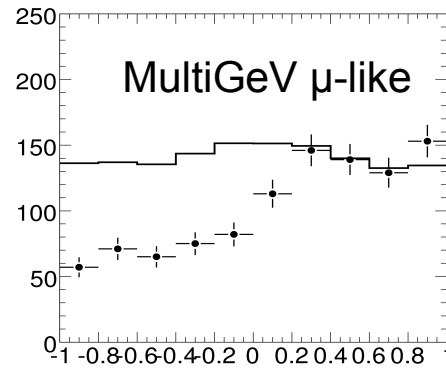
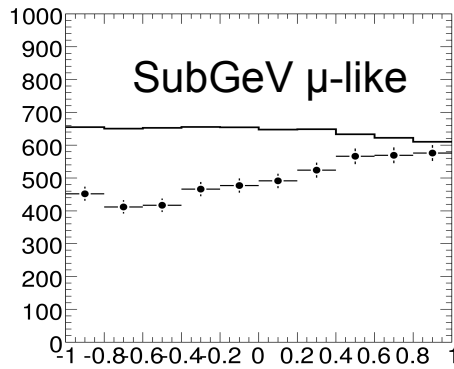
- Large ranges of L and E
- Various matter densities
- ⇒ great advantages for studying exotic phenomena

Atmospheric Neutrino Observations

Number of Events

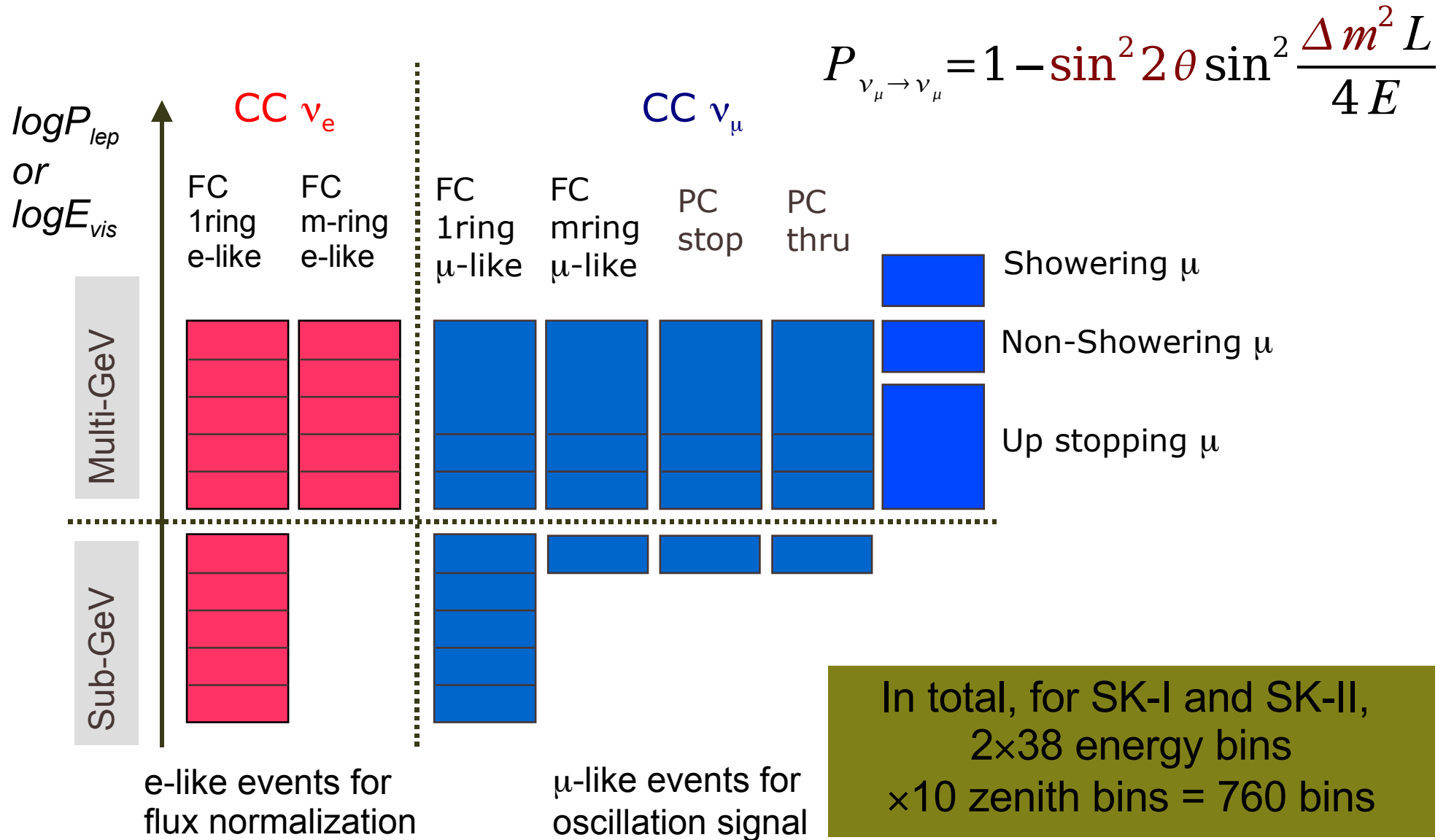


● observation
— Null oscillation prediction



$\cos\theta$

Data Analysis: Binning



Data Analysis: Pull Method

$$\chi^2 = \sum_{i=1}^N 2(N_i^{\text{exp}} - N_i^{\text{obs}} - N_i^{\text{obs}} \ln \frac{N_i^{\text{obs}}}{N_i^{\text{exp}}}) + \sum_{j=1}^M \left(\frac{\epsilon_j}{\sigma_j} \right)^2$$

Data bins: likelihood ratio

Systematic uncertainties: Gaussian

Expected number of events

Expected number of events without considering systematics

$$\begin{cases} N_i^{\text{exp}} = \left(1 + \sum_{j=1}^M f_i^j \epsilon_j \right) N_i^{\text{exp0}} \\ N_i^{\text{exp0}} = P_{\text{survival}}(\text{model x with parameters } \vec{x}) N_i^{\text{nosc}} \end{cases}$$

Survival probability predicted by model x

Null oscillation prediction

Plug in different models and find the minimum chi-squares

Combining SK-I and SK-II

- Data bins are considered as independent observations
- Systematic uncertainties

→ Identical for SK-I and SK-II

Atm neutrino flux (14)

Neutrino interaction (12)

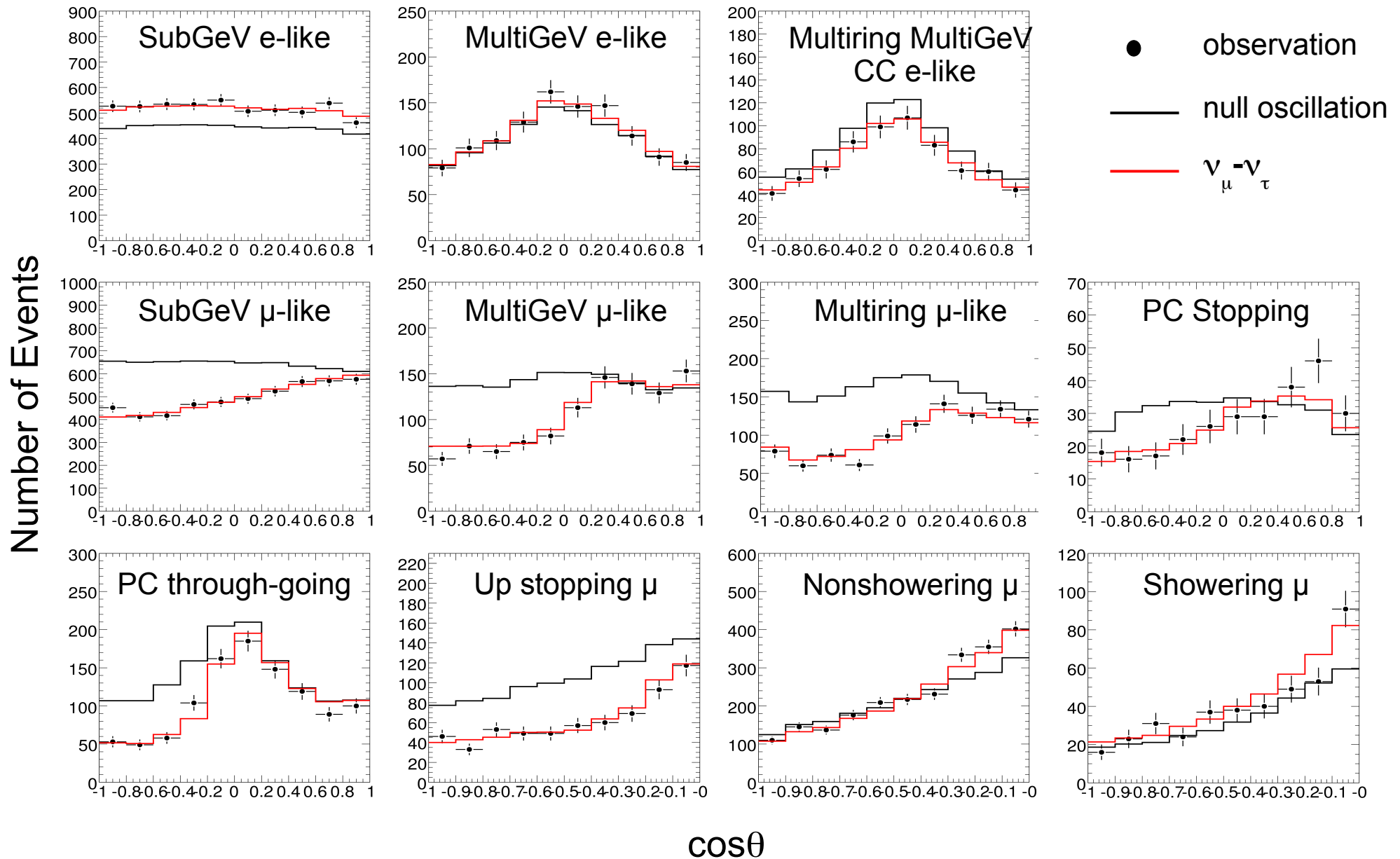
→ Independent for SK-I and SK-II

Solar activity (1)

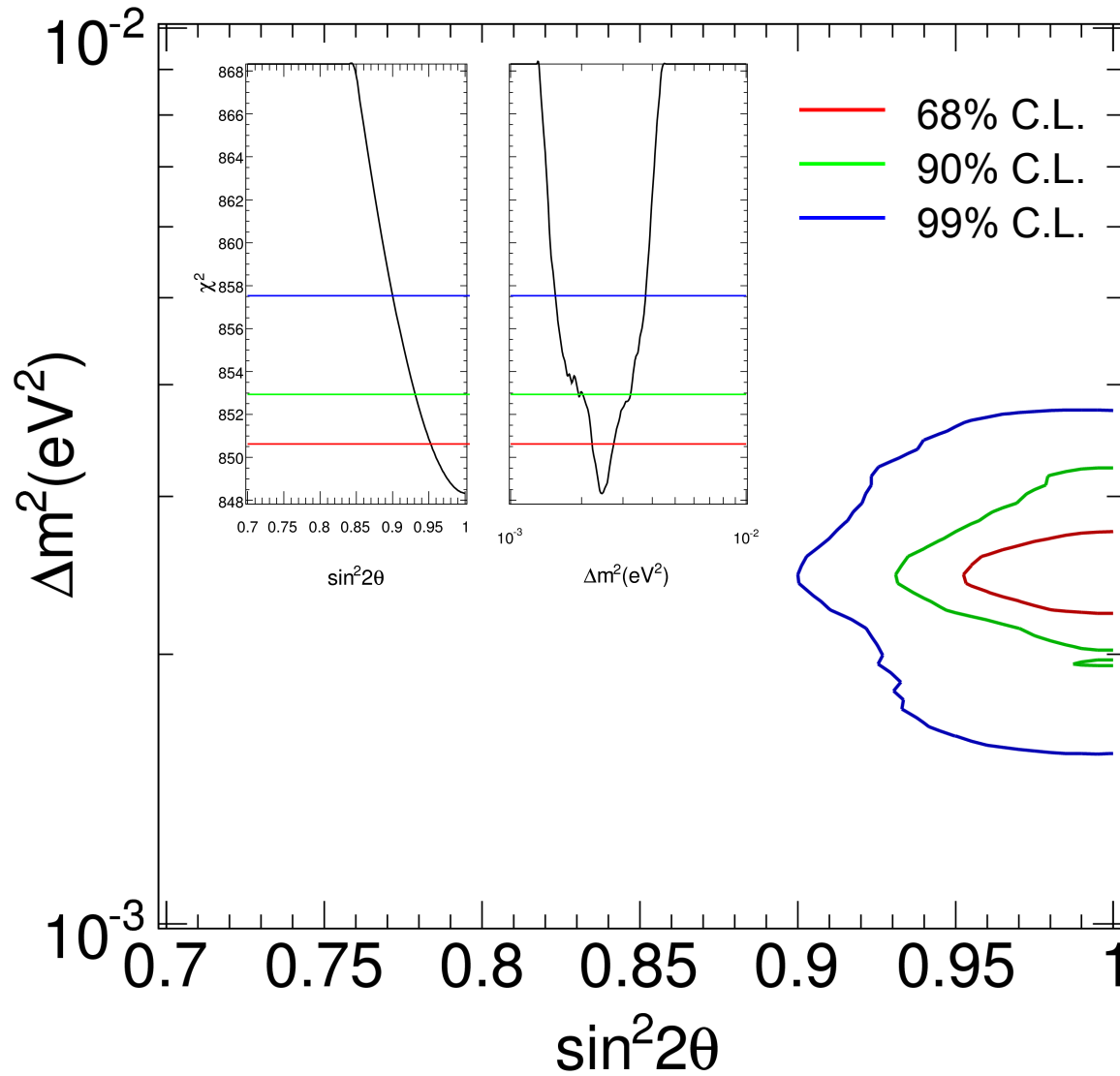
Data selection and
event reconstruction (21)

→ In total, 70 systematic uncertainties for SK-I and SK-II combined analysis

Zenith Distribution Explained by $\nu_{\mu} \rightarrow \nu_{\tau}$ Oscillation



Standard Mixing Parameters



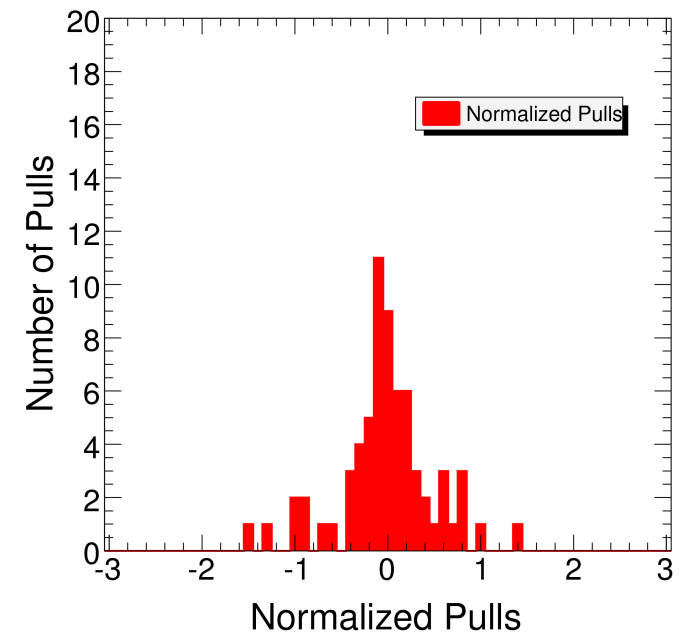
$$\nu_{\mu} \rightarrow \nu_{\tau}$$

$$\sin^2 2\theta = 1$$

$$\Delta m^2 = 2.5 \times 10^{-3} \text{ eV}^2$$

$$\chi^2 / \text{dof} = 839.7 / 755$$

$$p\text{-value} = 18\%$$



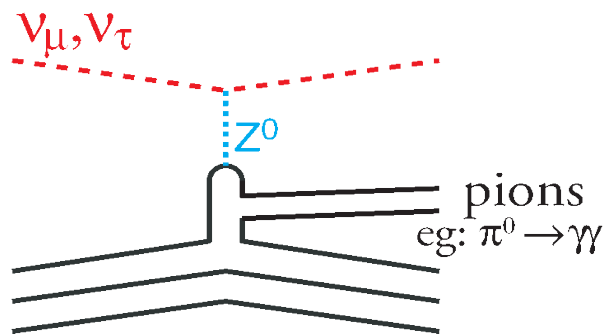
Must It Be Tau Neutrino?

- If three flavors of neutrinos, there is no choice
 - A ν_μ - ν_e oscillation does not explain the Super-K observation
 - Chooz and Palo Verde: no oscillation at the scale $\Delta m^2 \sim 10^{-3} \text{eV}^2$
- LEP experiments: Z decay width consistent with 3 neutrino flavors, $N_\nu = 2.992 \pm 0.020$
- ➔ But sterile neutrinos (ν_s : no electric, strong or weak charge) can still fit in the picture
 - Some theoretical models do predict the existence of sterile neutrinos
 - Some data are in favor of the existence of sterile neutrinos
 - ✓ Sterile neutrino may solve the LSND anomaly
 - ✓ Sterile neutrino can help solve the nuclear synthesis problem during the supernova R-process

Signatures of the Sterile Neutrinos

Based on the definition of sterile neutrino, ν_μ - ν_τ oscillation can be distinguished from ν_μ - ν_s oscillation in two ways

1. A trivial difference: neutral current events

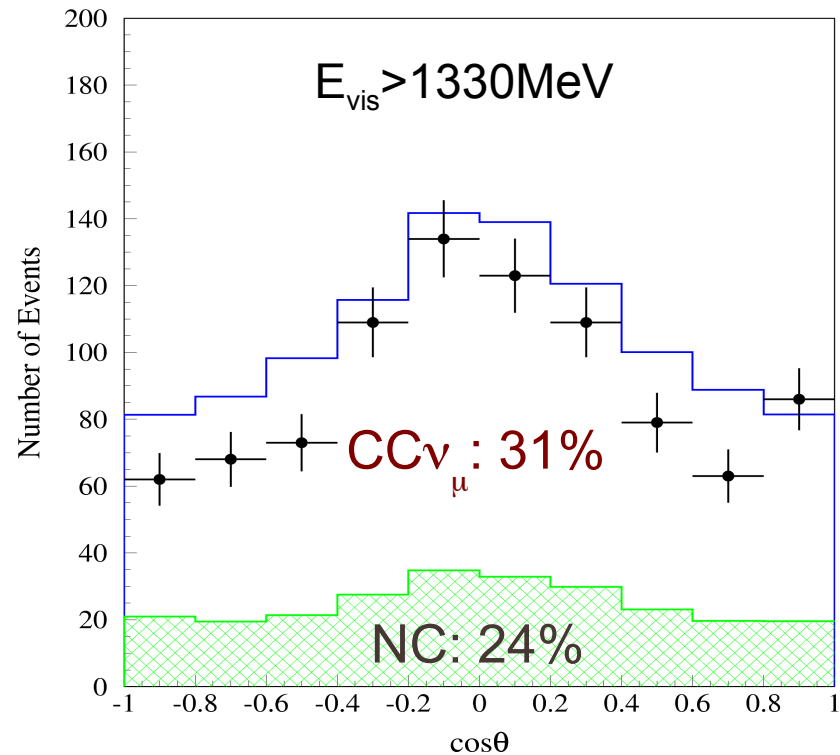
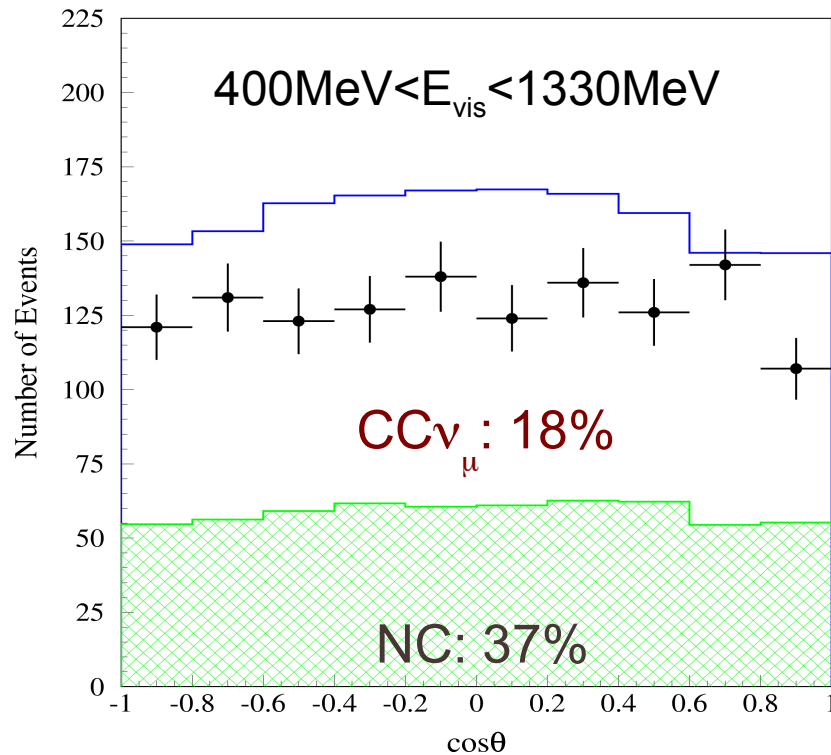


ν_s : no interaction

2. A more subtle effect: Matter Effect

1. NC Events at Super-K

- Multi-ring events: neutral pions are the NC signature at SK
- Brightest ring e-like
- $E_{\text{vis}} > 400\text{MeV}$: Low energy events do not point well



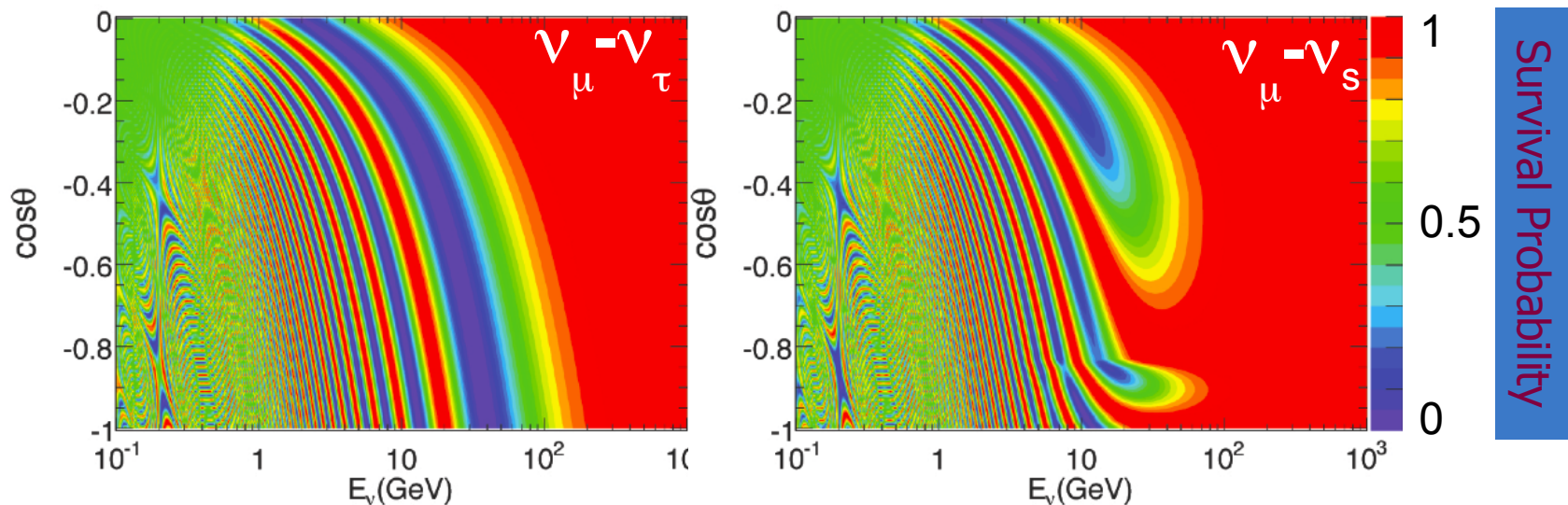
2. Matter Effect

- If two neutrino flavors interact differently in matter

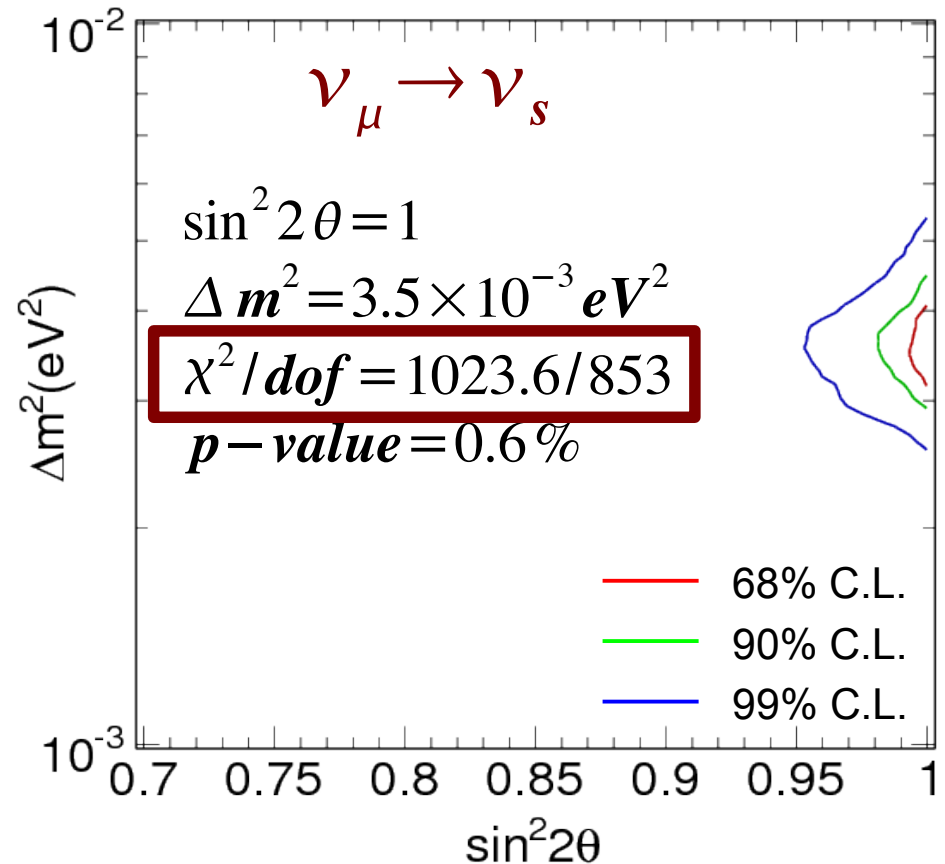
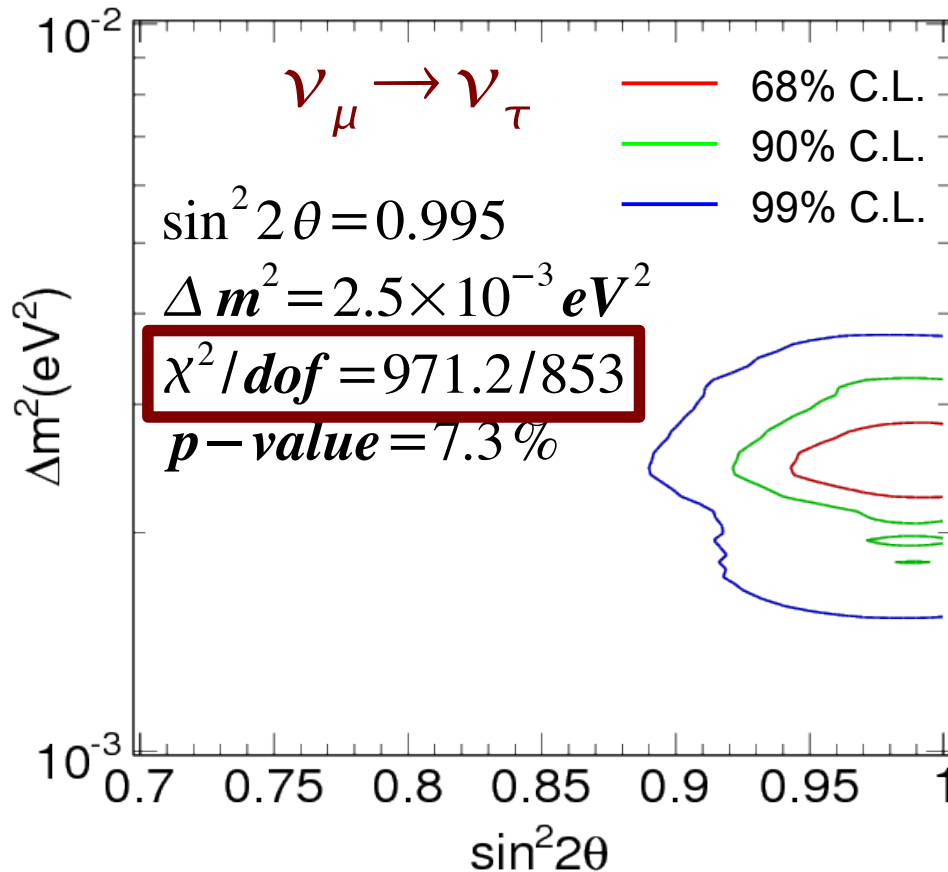
$$P_{osc} = \sin^2 2\theta_M \sin^2 \frac{\Delta m_M^2 L}{4E} \quad \left\{ \begin{array}{l} \sin^2 2\theta_M = \frac{\sin^2 2\theta}{(2E\Delta V/\Delta m^2 - \cos 2\theta)^2 + \sin^2 2\theta} \\ \Delta m_M^2 = \Delta m^2 \sqrt{(2E\Delta V/\Delta m^2 - \cos 2\theta)^2 + \sin^2 2\theta} \end{array} \right.$$

- $\nu_\mu - \nu_s$: ν_μ and ν_s interact with matter differently $\Delta V = \mp \sqrt{2} G_F \frac{\rho_n}{2}$
 \Rightarrow matter effect \Rightarrow oscillation is suppressed

Survival probability of ν_μ crossing Earth: $\Delta m^2 = 2.5 \times 10^{-3} \text{eV}^2$, $\sin^2 2\theta = 1$



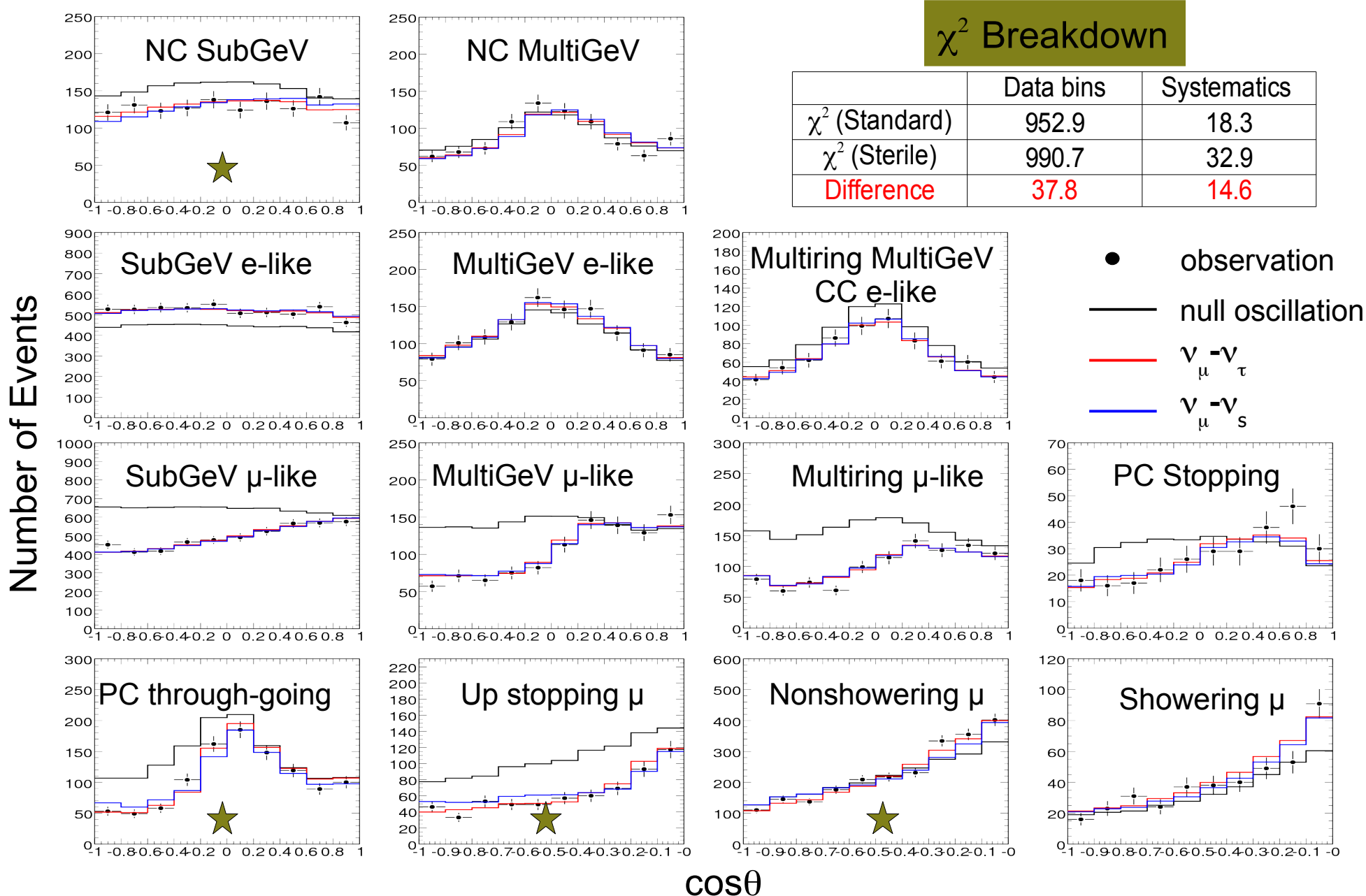
Tau Neutrino vs Sterile Neutrino



P-values calculated using toy MC method.

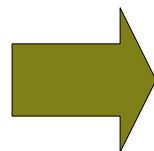
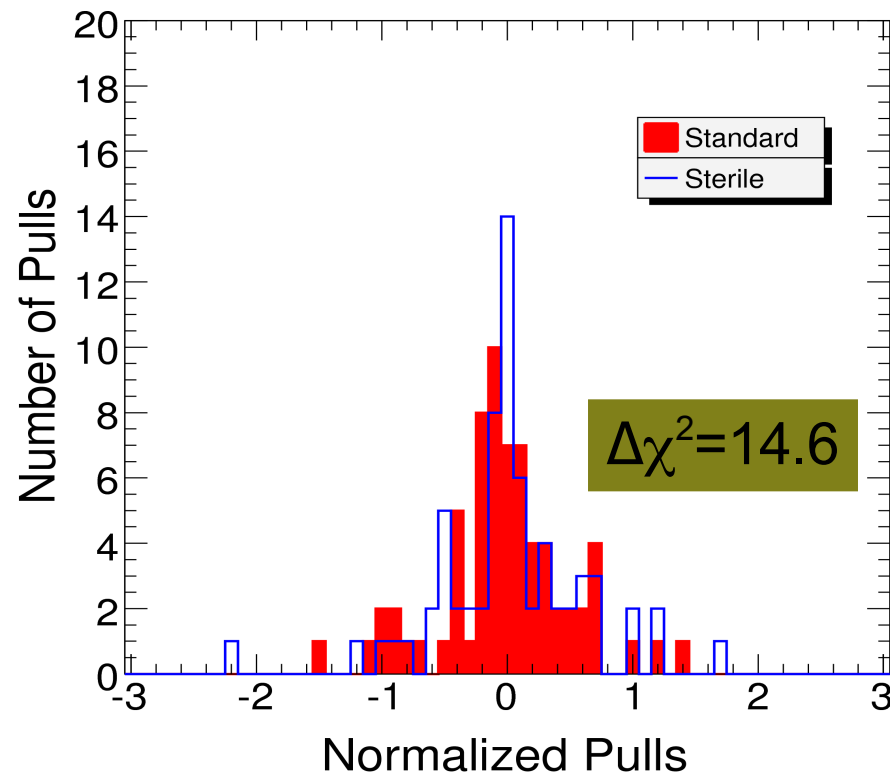
- Exclusion Level: 7.2σ

Comparison of Zenith Distributions



$\Delta\chi^2$ Contribution Breakdown

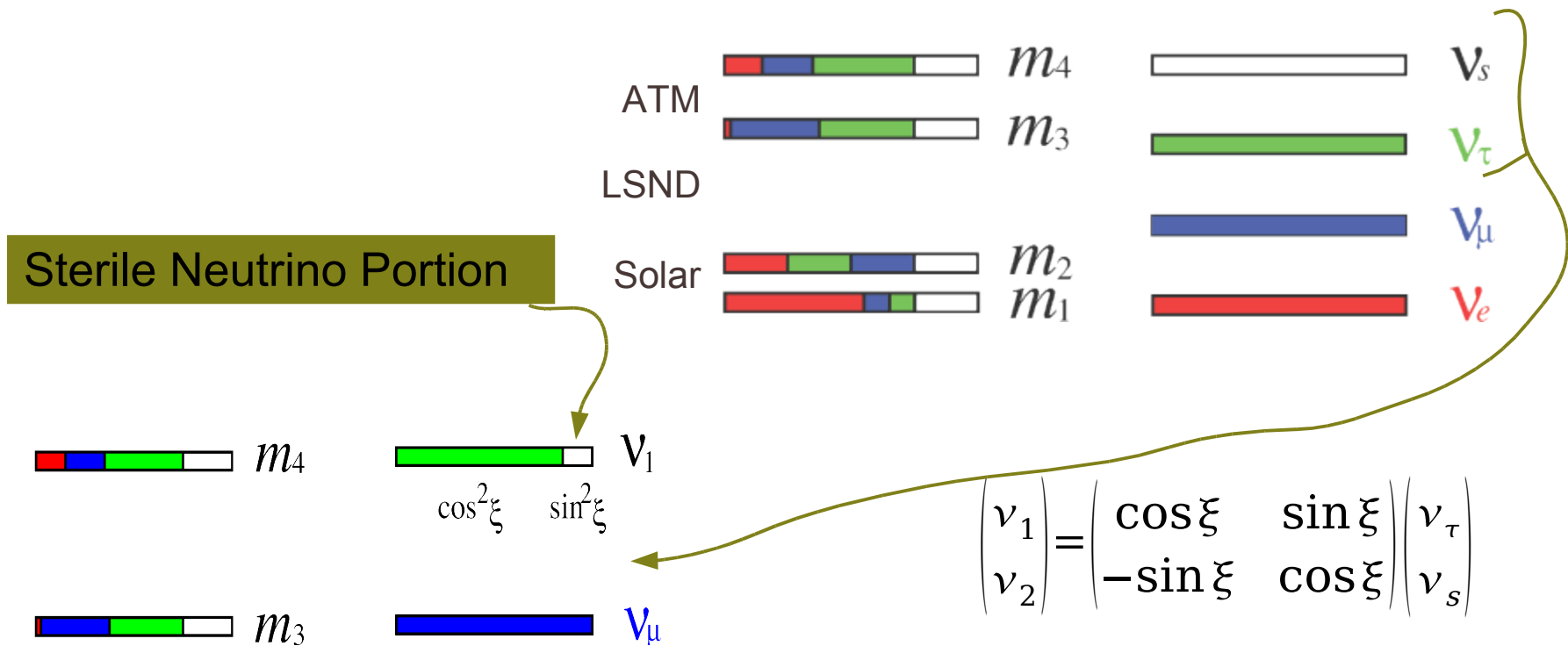
Single Ring SubGeV e-like	0.8
Single Ring MultiGeV e-like	-2.1
Multi-Ring MultiGeV CC e-like	0.8
Single Ring SubGeV μ -like	-1.3
Single Ring MultiGeV μ -like	-2
Multi-Ring μ -like	3.8
NC-Enhanced SubGeV	5
NC-Enhanced MultiGeV	1.2
PC Stopping μ	2.9
PC Through-Going μ	12.3
Upward Stopping μ	7.2
Upward NonShowering μ	11.2
Upward Showering μ	-1.5
TOTAL	37.8



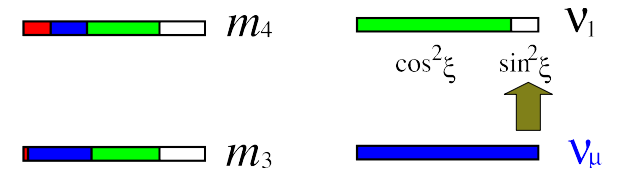
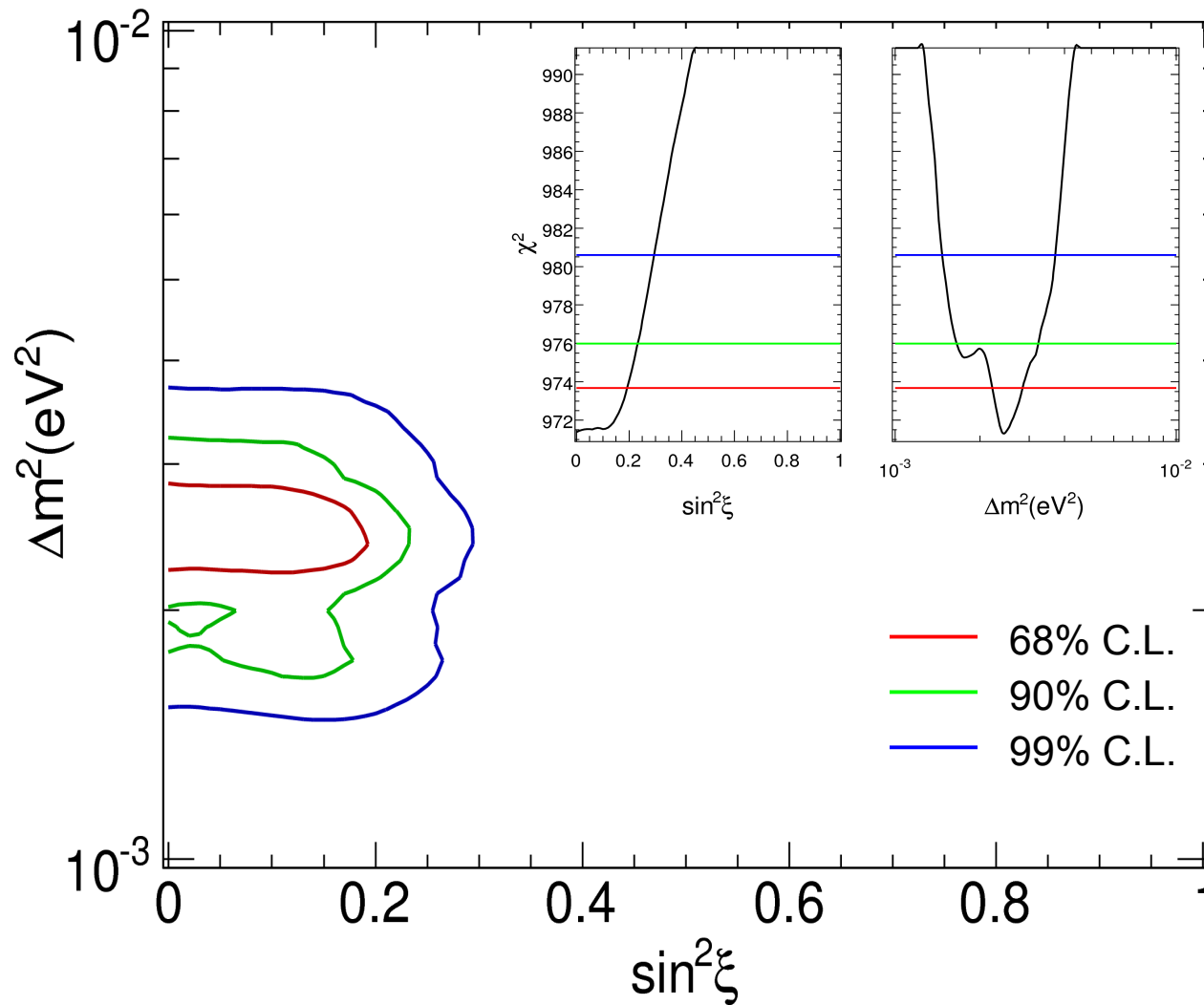
- The right energies and baselines of those events give the strongest matter effects

An Admixture Case

- Admixtures are model dependent
- This analysis is base on Fogli *et al* PRD 63(053008), 2001
 - A 2+2 mass hierarchy model
 - Constructing two superposition states of ν_s and $\nu_\tau \rightarrow$ two flavor mixing



Admixture Allowance



• Allowed sterile
 neutrino admixture
 limit at 90% C.L.:
 $\sin^2 \xi < 23\%$

Violations of Lorentz and CPT Invariance

→Neutrino oscillations without masses

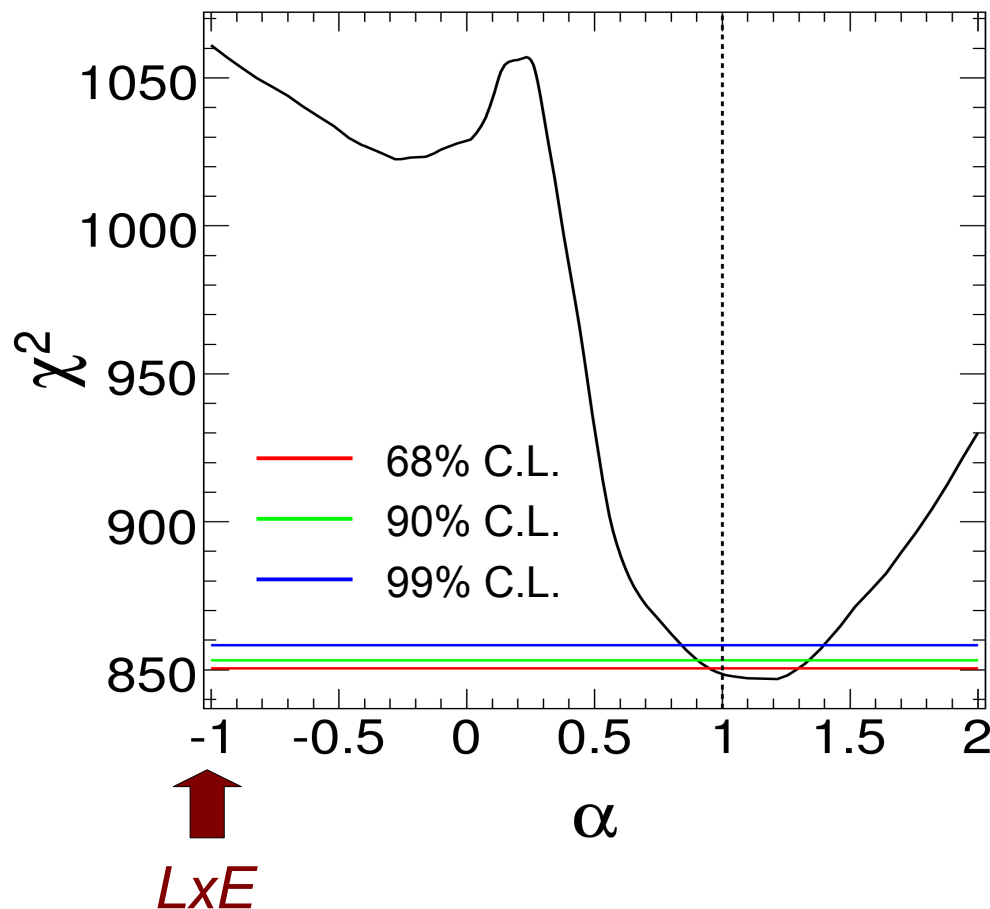
- Oscillation is caused by modified dispersion relation

→Important fundamental symmetries

- Broken at some high energy level? (e.g. Quantum Gravity)
- SK neutrino energies and pathlengths provide advantages checking them
- Minimal Standard Model Extension constructed by Kostelecky *et al*, hep-ph/0403088
 - $\mathcal{L} = a_{\mu AB} \bar{L}_A \gamma^\mu L_B + \frac{1}{2} i c_{\mu\nu AB} \bar{L}_A \gamma^\mu \overleftrightarrow{D}^\nu L_B$
 - The first term violates both CPT (CPTV) and Lorentz invariance (LIV); the second term only violates Lorentz invariance
 - Two rotationally invariant cases (only time components non-zero)
 - Coleman and Glashow, PRD 59(116008), 1999
 - Barger *et al*, PRL 85(5055), 2000

Lorentz Invariance Violation

- $-C_{AB}^{TT}(L_A \gamma^0 \partial^0 L_B + \partial^0 L_A \gamma^0 L_B) \Rightarrow \sin^2(\Delta c L E)$ oscillation
 - Mixing between different “maximum attainable velocity” eigenstates
- A more general form: $P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \sin^2 2\theta \sin^2 \kappa L/E^\alpha$



- LxE oscillation is strongly disfavored
 - Excluded at $\sim 14\sigma$
- L/E is within the $1^{\text{st}}\sigma$
 - $1.16 + 0.14 / -0.21$
- A natural question: what is the scale LIV might appear?

LIV as a Sub-Dominant Effect

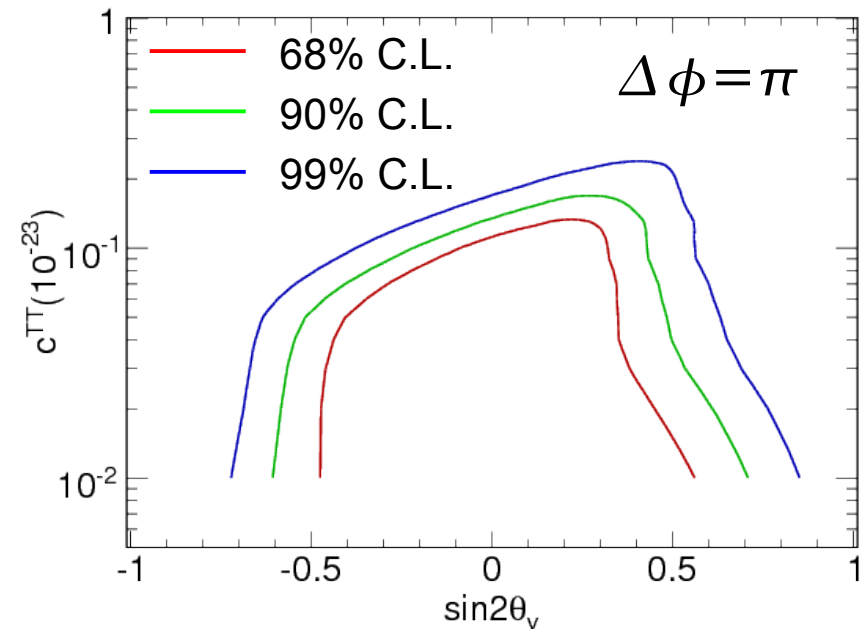
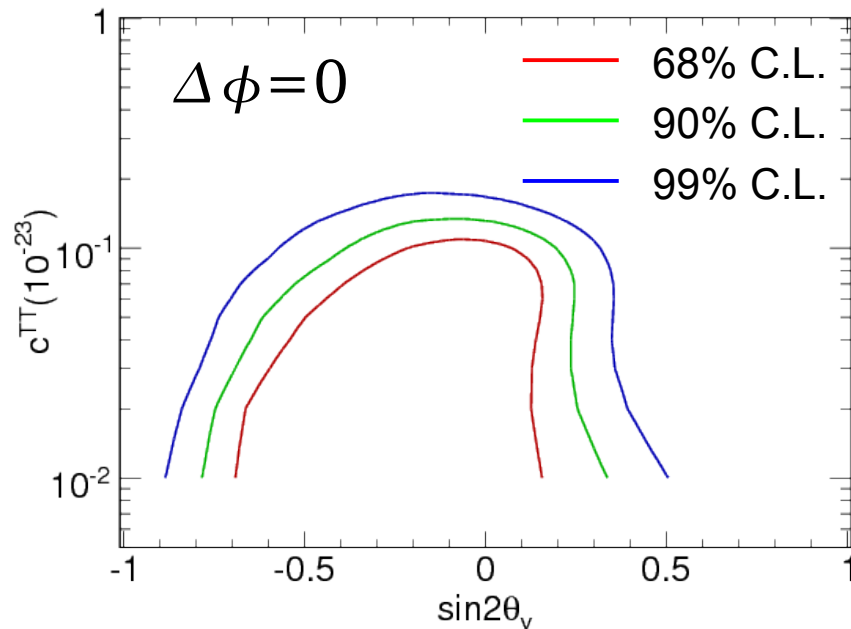
- Considering LIV as a sub-dominant effect
- Assuming best-fit parameter values for the standard oscillation

$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \sin^2 2\Theta \sin^2 \Omega$$

$$\left\{ \begin{array}{l} \tan 2\Theta = \frac{1 + (E/E_c)^2 \sin 2\theta_v}{(E/E_c)^2 \cos 2\theta_v} \\ \Omega = 1.27 \sqrt{(\Delta m^2 L/E)^2 \pm 4c^{TT} \sin 2\theta_v L E + 4(c^{TT} L E)^2} \\ E_c = \sqrt{\frac{\Delta m^2}{2c^{TT}}} \end{array} \right.$$

- c^{TT} : the difference of maximum attainable velocities
- θ_v : mixing angle between two different maximal attainable velocity eigenstates
- “+/-”: the $0/\pi$ phase difference between the mass mixing matrix and the maximum attainable velocity mixing matrix

Limits on LIV Scale



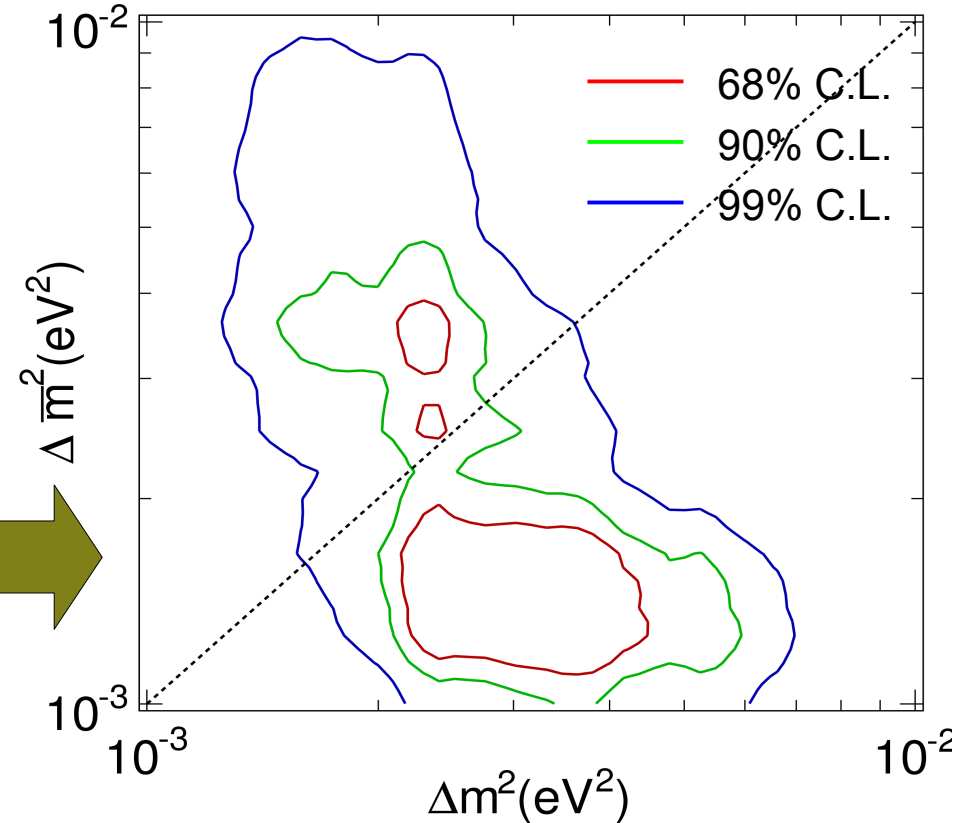
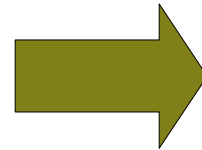
- $\Delta\phi=0$: $c^{TT} < 1.2 \times 10^{-24}$ at 90% C.L.
 - $\sin 2\theta_v = -0.12$; $c^{TT} = 0.05 \times 10^{-23}$
- $\Delta\phi=\pi$: $c^{TT} < 1.3 \times 10^{-24}$ at 90% C.L.
 - $\sin 2\theta_v = -0.02$; $c^{TT} = 0.06 \times 10^{-23}$

- Limits from other experiments
 - Cosmic ray spectrum:
 $\sim 10^{-15}(\gamma)$, $\sim 10^{-23}(p)$
 - Nuclear magnetic resonance frequencies:
 $\sim 10^{-21}(e)$, $\sim 10^{-30}(n)$

An ad hoc CPT Violation Test

$$P_{\nu_\mu \rightarrow \nu_\mu / \bar{\nu}_\mu \rightarrow \bar{\nu}_\mu} = 1 - \sin^2 2\theta \sin^2 \left(\frac{(\Delta m^2 / \Delta \bar{m}^2) L}{4E} \right)$$

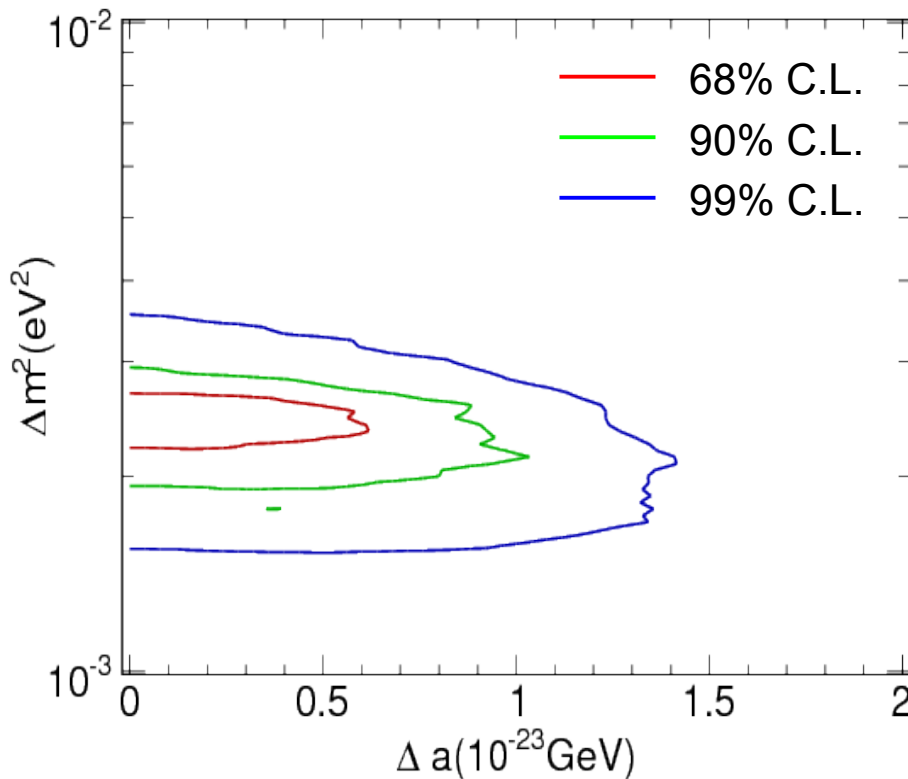
- **Simple assumption:** neutrinos and antineutrinos could have different mass squared splittings
 - Mainly triggered by the LSND
- **Question: Is this allowed by SK?**
 - Assuming maximal mixing
 - Allowing neutrinos and antineutrinos mass squared splittings change independently
- Best-fit: $\begin{cases} \sin 2\theta = 1 \\ \Delta m^2 = 3.7 \times 10^{-3} \text{ eV}^2 \\ \Delta \bar{m}^2 = 1.5 \times 10^{-3} \text{ eV}^2 \end{cases}$



Super-K best-fit is far away from the LSND scale
 → then, what is energy level CPTV effects could appear?

Limit on CPT Violation Scale

- $-\mathbf{a}_{AB}L_A\gamma^0L_B \Rightarrow \Delta\mathbf{a}L$ oscillation
- **As a sub-dominant effect** $\Rightarrow P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \sin^2 2\theta \sin^2\left(\frac{\Delta m^2}{4E} \pm \Delta\mathbf{a}\right)L$
- Assuming maximal mixing for the mass eigenstates



- At 90% C.L.: $\Delta\mathbf{a} < 1.05 \times 10^{-23} \text{ GeV}$

- Limits from other experiments

Barger *et al*, PRL 85(5055), 2000

- $g-2$: $\sim 10^{-23} \text{ GeV}$
- $K^0 - \bar{K}^0$: $\sim 0.44 \times 10^{-18} \text{ GeV}$

How Can Neutrinos Simply Vanish?

- **Neutrino decoherence**

- Quantum systems can go out of coherence by interacting with the environment → “disappearance” of coherent quantum states (e.g. quantum gravity effect)

- $$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \frac{1}{2} \sin^2 2\theta \left(1 - e^{-\gamma L} \cos \frac{\Delta m^2 L}{2E} \right)^2$$
 - γ may have energy dependence: $\gamma = \gamma_0 (E/\text{GeV})^n$
 - **Pure decoherence (n=-1):** $\Rightarrow P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \frac{1}{2} (1 - e^{-\gamma L/E})^2$

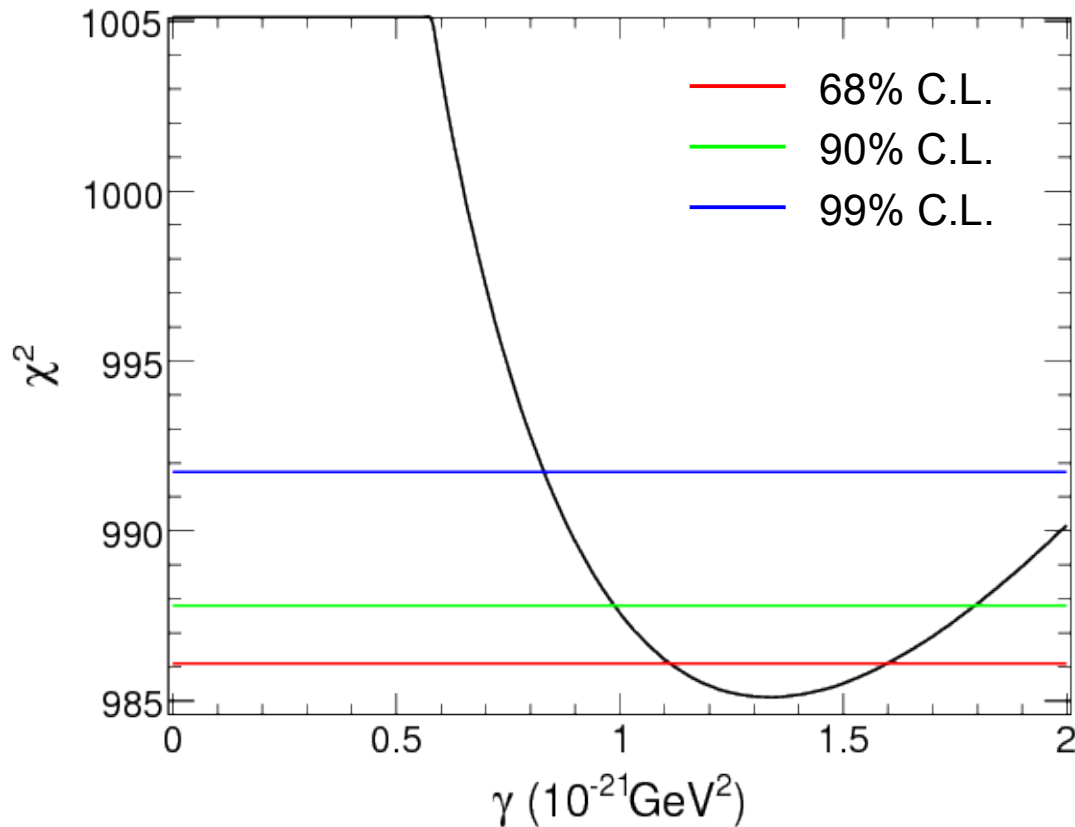
- **Neutrino decay**

- “There is no reason to assume mass eigenstates are stable”

- $$P_{\nu_\mu \rightarrow \nu_\mu} = \sin^4 \theta + e^{-\alpha L/E} \cos^4 \theta + 2 \sin^2 \theta \cos^2 \theta e^{-\alpha L/2E} \cos \frac{\Delta m^2 L}{2E}$$
 - **Pure decay case :** $\Delta m^2 \rightarrow 0 \Rightarrow P_{osc} = (\sin^2 \theta + e^{-\alpha L/2E} \cos^2 \theta)^2$

Model Comparison: Decoherence

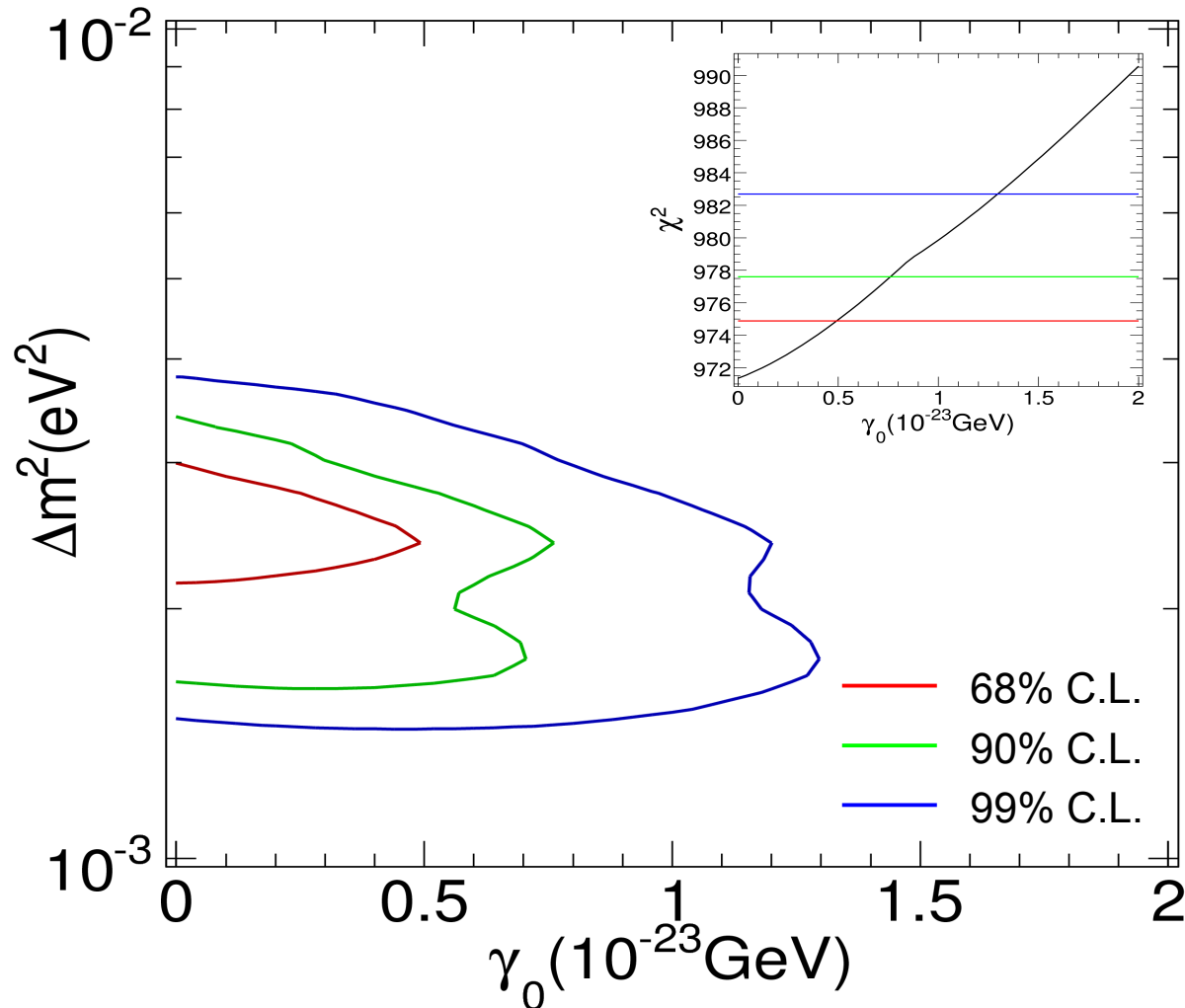
$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \frac{1}{2} \sin^2 2\theta (1 - e^{-\gamma L/E})^2$$



- Best fit
 - $\gamma = 1.3 \times 10^{-21} \text{ GeV}^2$
 - $\sin^2 2\theta = 1$
 - $\chi^2/\text{dof} = 987/853$
- $\Delta\chi^2 = 16$
 $\Rightarrow 4\sigma$ exclusion level
- Neutrino decoherence does not explain SK atmospheric neutrino observation as well as the $\nu_\mu - \nu_\tau$ oscillation

Limits on Decoherence Parameter (I)

$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \frac{1}{2} \sin^2 2\theta \left(1 - e^{-\gamma_0 L} \cos \frac{\Delta m^2 L}{2E} \right)^2$$

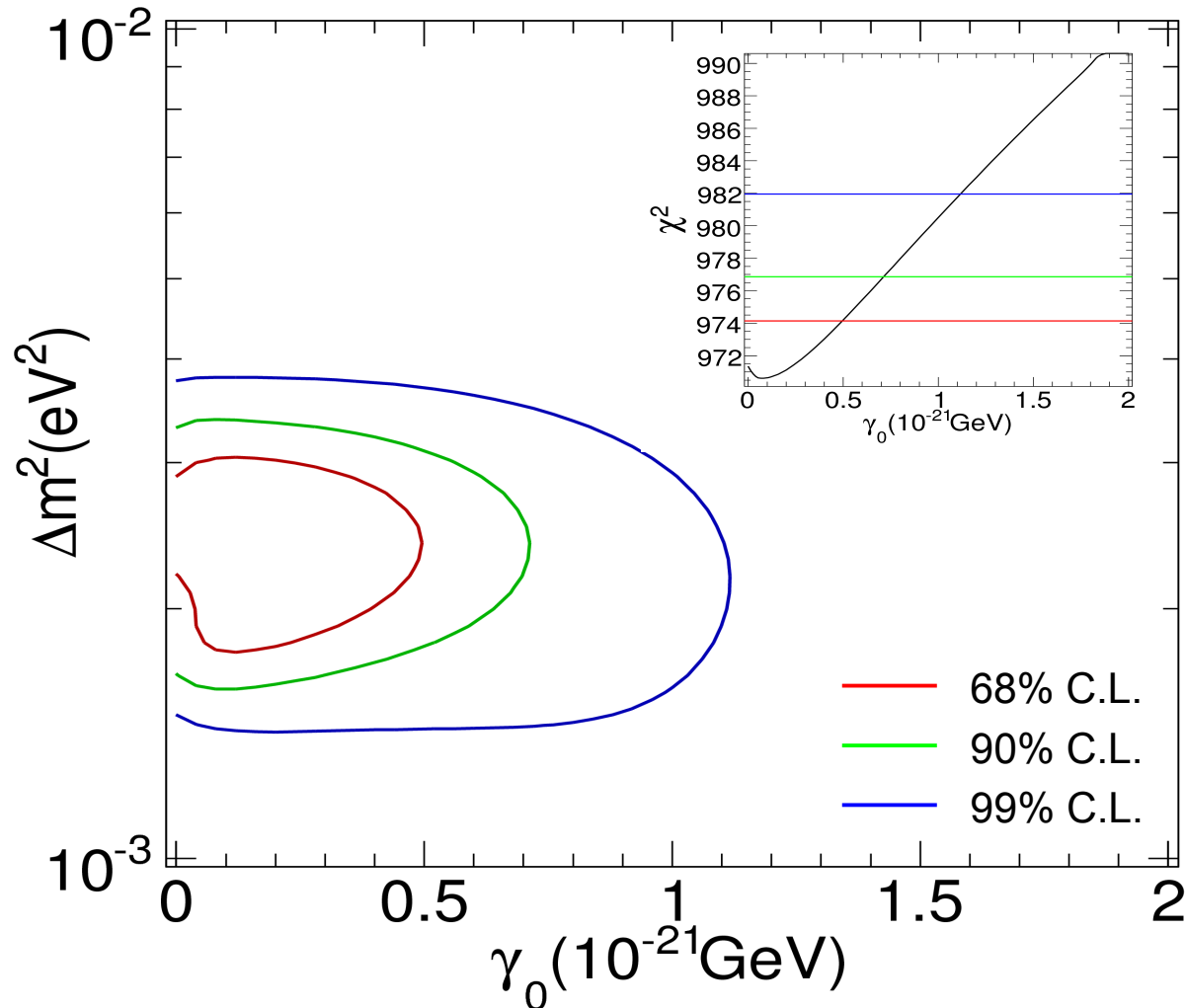


- $\gamma = \gamma_0$: most trivial case
- Best fit
 - $\gamma_0 = 0$.
 - $\sin^2 2\theta = 1$
 - $\Delta m^2 = 2.4 \times 10^{-3} \text{ eV}^2$
 - $\chi^2/\text{dof} = 971/853$

At 90% C.L., the
allowed limit:
 $\gamma_0 < 0.76 \times 10^{-23} \text{ GeV}$

Limits on Decoherence Parameter (II)

$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \frac{1}{2} \sin^2 2\theta (1 - e^{-\gamma_0 L/(E/\text{GeV})} \cos \frac{\Delta m^2 L}{2E})^2$$

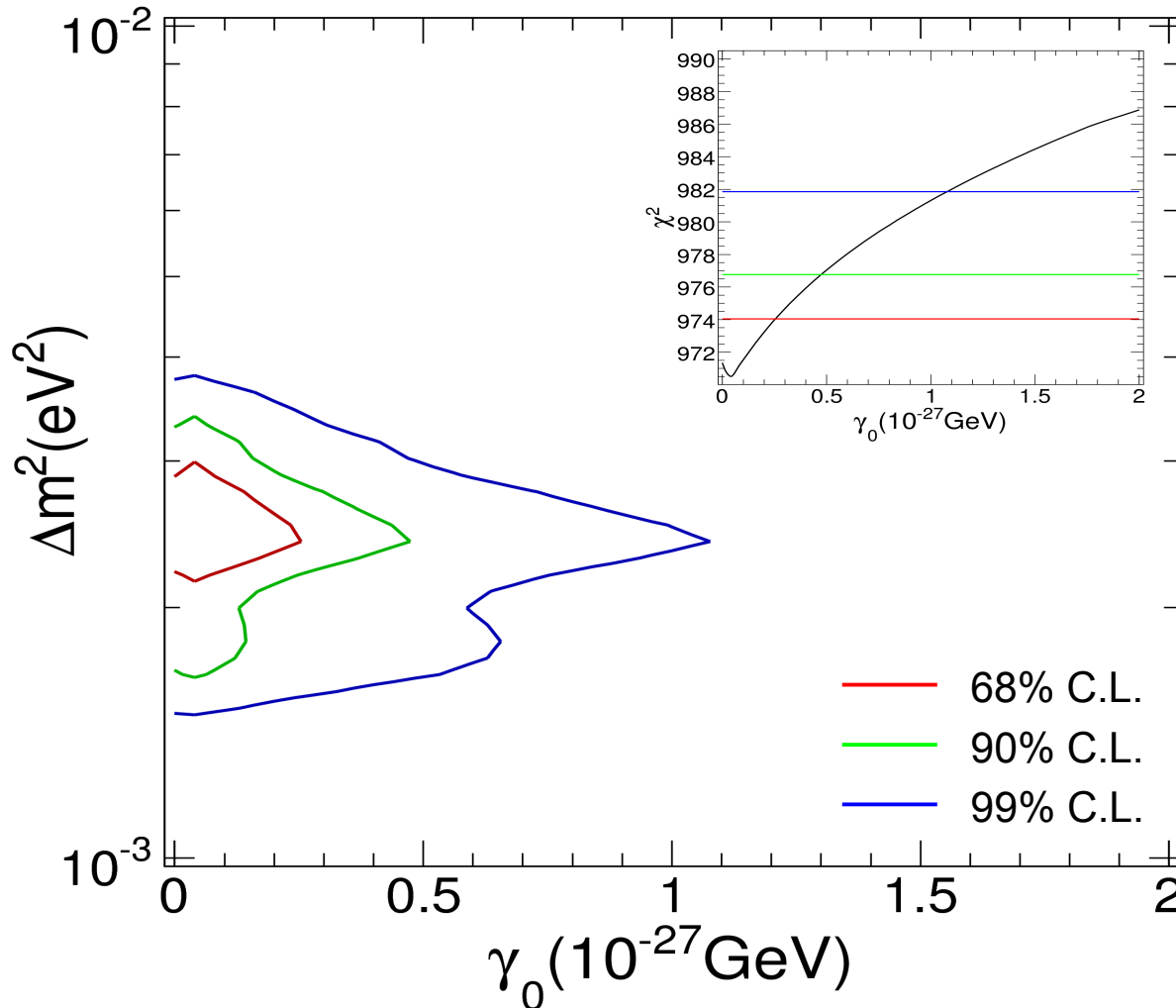


- $\gamma = \gamma_0 / (E/\text{GeV})$
- Best fit
 - $\gamma_0 = 0.08 \times 10^{-21} \text{GeV}$
 - $\sin^2 2\theta = 1$
 - $\Delta m^2 = 2.4 \times 10^{-3} \text{eV}^2$
 - $\chi^2/\text{dof} = 971/853$

At 90% C.L., the allowed limit:
 $\gamma_0 < 0.61 \times 10^{-21} \text{GeV}$

Limits on Decoherence Parameter (III)

$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \frac{1}{2} \sin^2 2\theta (1 - e^{-\gamma_0 L (E/\text{GeV})^2} \cos \frac{\Delta m^2 L}{2E})^2$$

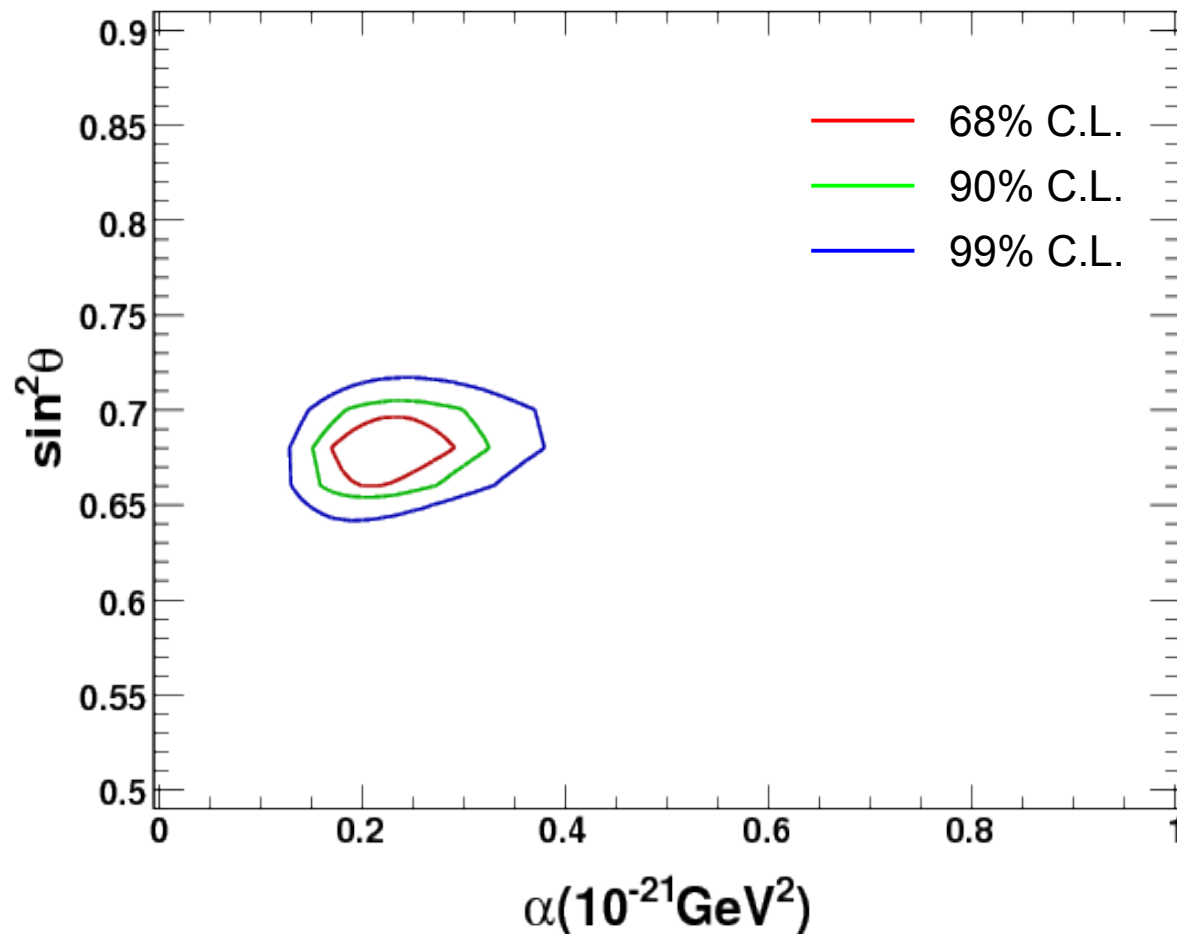


- $\gamma = \gamma_0 (E/\text{GeV})^2$
- Best fit
 - $\gamma_0 = 0.04 \times 10^{-27} \text{ GeV}$
 - $\sin^2 2\theta = 1$
 - $\Delta m^2 = 2.4 \times 10^{-3} \text{ eV}^2$
 - $\chi^2/\text{dof} = 971/853$

At 90% C.L., the
allowed limit:
 $\gamma_0 < 4.8 \times 10^{-28} \text{ GeV}$

Model Comparison: Neutrino Decay

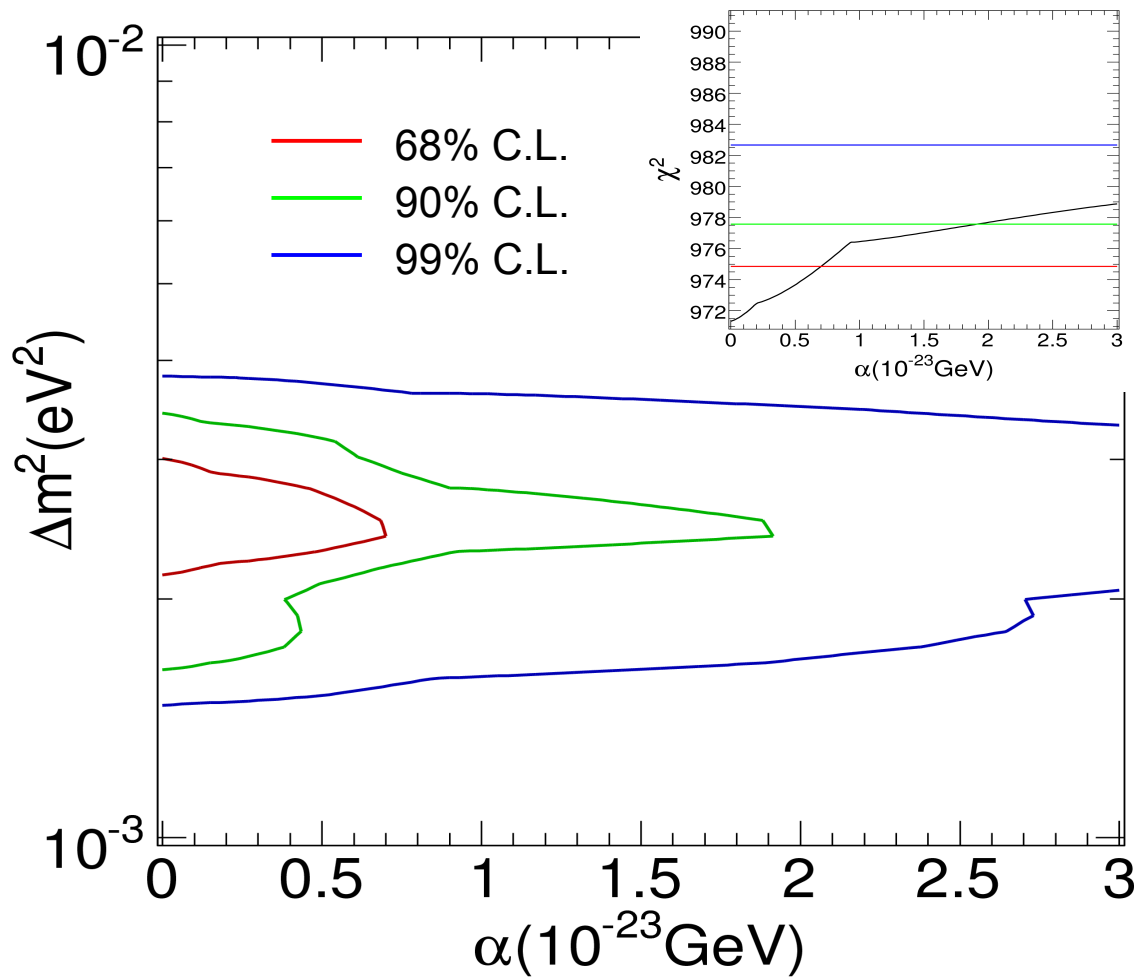
$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - (\sin^2 \theta + e^{-\alpha L/2E} \cos^2 \theta)^2$$



- Best fit
 - $\sin^2 \theta = 0.68$
 - $\alpha = 2.2 \times 10^{-22} \text{GeV}^2$
 - $\chi^2/\text{dof} = 983/853$
- $\Delta\chi^2 = 12$
 $\Rightarrow 3.5\sigma$ exclusion level
- Neutrino decay does not explain SK atmospheric neutrino observation as well as the $\nu_\mu - \nu_\tau$ osc.

Limits on Neutrino Decay Parameter

$$P_{\nu_\mu \rightarrow \nu_\mu} = \sin^4 \theta + e^{-\alpha L/E} \cos^4 \theta + 2 \sin^2 \theta \cos^2 \theta e^{-\alpha L/2E} \cos \frac{\Delta m^2 L}{2E}$$



- Best fit

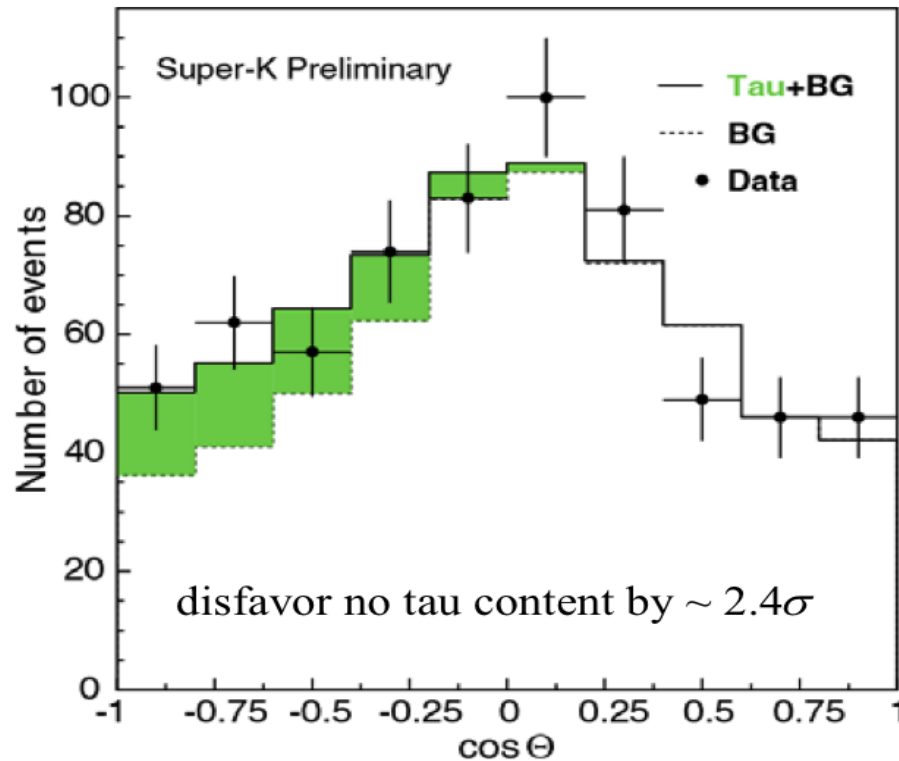
- $\alpha=0$
- $\sin^2 \theta=0.45$
- $\Delta m^2=2.4 \times 10^{-3} \text{ eV}^2$
- $\chi^2/\text{dof}=971/853$

At 90% C.L., the
allowed limit:
 $\alpha < 1.9 \times 10^{-23} \text{ GeV}^2$

Summary and Conclusions

- ν_μ - ν_τ oscillation analysis is carried out using SK-I+II atm ν data
 - $\sin^2 2\theta > 0.95$, $2.2 \times 10^{-3} \text{eV}^2 < \Delta m^2 < 2.7 \times 10^{-3} \text{eV}^2$
- ν_μ - ν_τ oscillation is compared with 3 kinds of alternatives:
 - ν_μ - ν_s oscillation: excluded at 7.2σ
 - Oscillation induced by LIV and CPTV are excluded
 - Neutrino decoherence and decay: excluded at 4σ and 3.5σ
- Atmospheric neutrino data can provide valuable constraints on scales of new physics beyond the Standard Model
 - An admixture 23% of ν_s is allowed at 90% C.L. (2+2 mass hierarchy)
 - LIV and CPTV limits are set: $\sim 10^{-24}$ and $\sim 10^{-23}$ GeV at 90% C.L.
 - Neutrino decoherence limits: $\sim 10^{-24}$ GeV, $\sim 10^{-22}$ GeV, and $\sim 10^{-28}$ GeV respectively for different energy dependence at 90% C.L.
 - Neutrino decay limit: $\sim 10^{-23}$ GeV² at 90% C.L.

Tau Event Searching



Statistically separate (NN & likelihood)
tau-like events in high energy sample;
look for up-down asymmetry
(after accounting for oscillation)

- Expected: $79 \pm 28(\text{sys})$
- Found:
 - Likelihood:
 $145 \pm 48(\text{stat}) + 15/-38(\text{sys})$
 - Neural Network:
 $152 \pm 47(\text{stat}) + 17/-29(\text{sys})$

No tau events assumption is
disfavored by $\sim 2.4\sigma$

Testing MaVaN

- Neutrinos gain mass only in high density matter (not in air or vacuum)

- Best Fit:

$$-\chi^2_{\text{MaVaN}} = 194.4/178 \text{ d.o.f}$$

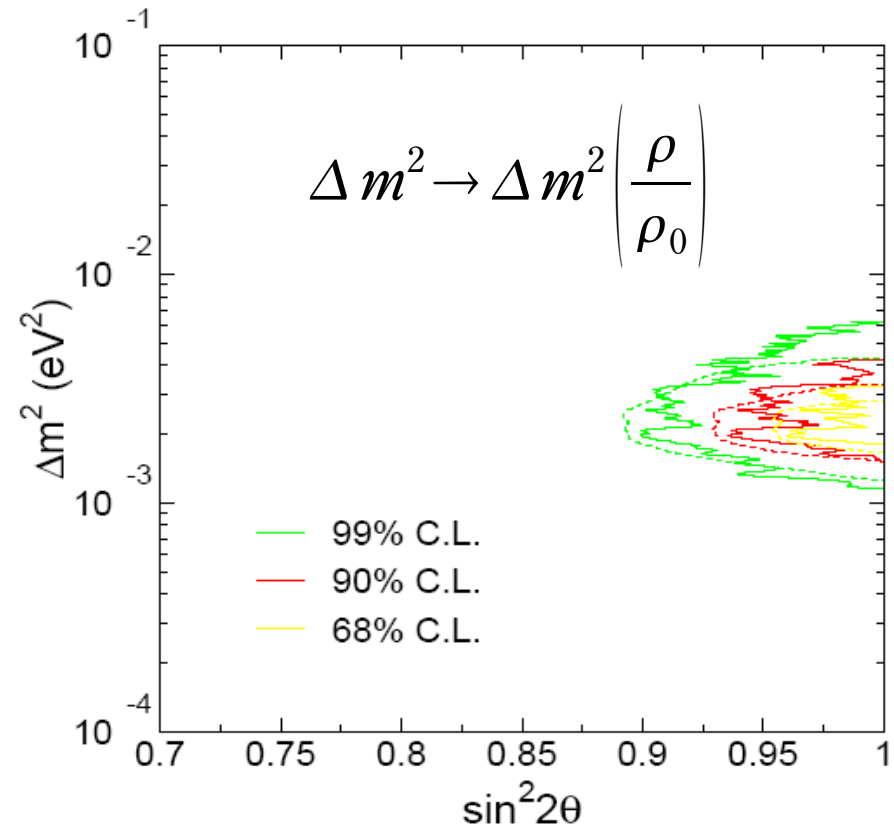
$$(\sin^2 2\theta, \Delta m^2) = (1.00, 2.19 \times 10^{-3} \text{ eV}^2)$$

$$-\chi^2_{\text{Standard}} = 174.97/178 \text{ d.o.f}$$

$$(\sin^2 2\theta, \Delta m^2) = (1.00, 2.11 \times 10^{-3} \text{ eV}^2)$$

- Excluded at 4.4σ level

Next step: $\Delta m^2 \rightarrow \Delta m^2 \left(\frac{\rho}{\rho_0} \right)^n$



----- Standard 2-flavor oscillations
—— MaVaN oscillations